

# Visible and infrared image registration using trajectories and composite foreground images

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## Abstract

The registration of images from multiple types of sensors (particularly infrared sensors and visible color sensors) is a step toward achieving multi-sensor fusion. This paper proposes a registration method using a novel error function. Registration of infrared and visible color images is performed by using the trajectories of moving objects obtained using background subtraction and simple tracking. The trajectory points are matched using a RANSAC-based algorithm and a novel registration criterion, which is based on the overlap of foreground pixels in composite foreground images. This criterion allows performing registration when there are few trajectories and gives more stable results. Our method was tested and its performance quantified using nine scenarios. It outperforms a related method only based on trajectory points in cases where there are few moving objects.

*Key words:* Infrared, Registration, multi-sensors, trajectories, foreground

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## 1. Introduction

Traditionally, the computer vision community has focused principally on processing images captured with visible range sensors (400-1000 nm) during day and in indoor environments. Because of their cost, infrared sensors (.9-13.5  $\mu\text{m}$ ) were used only in special area like medicine (breast cancer detection) and military (night vision). Infrared sensors are now becoming valuable assets in an advance surveillance system as they supply information that a visible sensor cannot provide in poor lighting, smoke, and fog. It is often useful to pair an infrared camera with a visible camera. They both perform well in different situations. For example, a visible camera fails when it is dark, but is good during the day. An infrared camera fails during very hot summer days (objects are undistinguishable), but otherwise is efficient in the dark. The two cameras are valuable in a video surveillance setup.

To benefit from both sensors, the fusion of information is often used. In many fusion techniques, registration is needed to find automatically the transformation matrix between two images or between two videos. In this paper, we are interested in registering two videos acquired from two cameras (one visible and one infrared) installed in a stereoscopic configuration and observing a common scene with an overlapping field of view. We assume that objects are in the same plane (i.e. that the scene is planar), that is, objects' distances from the camera are much larger than the camera baseline. We are particularly interested in the case for which the two cameras produce useful data, for example, during the day. In this situation, two images are

24 obtained, and thus the registration can be found to be used later on to  
25 improve monitoring of a scene in various in various lighting and weather  
26 conditions.

27 In this paper, we are dealing with the issue of evaluating a transforma-  
28 tion matrix based on a registration using trajectories [1, 2, 3]. Previous  
29 works use Euclidean distance between trajectory points as an error func-  
30 tion for evaluation, but it requires more trajectories to constrain the possible  
31 transformations. Furthermore, in our case, we do not wish to estimate the  
32 registration of a recorded video. We aim to register two cameras online as  
33 an automatic procedure that can be applied periodically over normal system  
34 operation. Thus, it is useful to find an evaluation criterion for finding the  
35 transformation matrix that does not require a large number of trajectories.

36 Our proposed registration method for infrared and visible color videos is  
37 based on the trajectories of moving objects obtained using background sub-  
38 traction and simple tracking. The videos from the two cameras are assumed  
39 to be synchronized. The trajectory points are matched using a RANSAC-  
40 based algorithm [4]. The novel registration criterion used in this algorithm  
41 is the number of overlapping foreground pixels in composite foreground im-  
42 ages. Note that we do not address the problem of fusion in this paper. We  
43 tested our method with the affine model, although it is applicable to any  
44 2D homography. Results are compared to ground-truth, and we show that  
45 using composite foreground images improve registration accuracy compared  
46 to using only distance on trajectory points. Furthermore, it gives more stable  
47 results. Because our proposed method aligns silhouettes instead of trajectory  
48 points, it is appropriate as automatic registration for methods performing im-

49 age fusion using blob contours or edges [5, 6], where the alignment of these  
50 structures is assumed and required.

51 Related works are discussed in section 2. Section 3 presents our method-  
52 ology and section 4 presents registration results and an accuracy evaluation  
53 with ground-truth. Finally, section 5 concludes the paper.

## 54 **2. Related works**

55 Most works related to this paper are about visible/infrared image regis-  
56 tration. For registering infrared and visible images, correspondences between  
57 images must be found. There are two types of approaches: 1) intensity-based  
58 methods, and 2) Feature-based methods [7]. These approaches have been de-  
59 veloped for visible stereo pairs, but several researchers have tried applying  
60 them to mixed infrared/visible pairs. Their application to this camera con-  
61 figuration is not straight forward since infrared and visible images are the  
62 manifestation of two different phenomena. Visible cameras measure reflected  
63 light on objects, while infrared camera measure principally infrared radiations  
64 emitted by objects. A texture or an edge in a visible image is often missing  
65 in the infrared image because texture seldom influences the heat emitted by  
66 an object.

### 67 *2.1. Approaches based on intensity*

68 Approaches based on intensity rely on either cross-correlation, on Fourier  
69 method, or on the mutual information theory. Cross-correlation (CC) match-  
70 ing is computed for pairs of windows in two images. A pair of windows  
71 that maximizes the cross-correlation is considered a correspondence [8]. This

72 method has some drawbacks which are the flatness of similarity measure in  
73 textureless areas and the high computational complexity.

74 The second matching approach is the Fourier method. The Fourier rep-  
75 resentation of edge images is exploited and correlations are found in the  
76 frequency domain [9]. It has robustness to noisy images and images that are  
77 captured under variable lighting conditions. It is relatively fast compared to  
78 correlation-like methods.

79 Finally, in mutual information theory methods [10, 11, 12, 13, 14], images  
80 from both sensors are transformed and overlapped in such a way to maximize  
81 the dependence between the two images. The mutual information is used as  
82 a quality metric to evaluate correspondence for a given transformation. How-  
83 ever, for two given infrared/visible image pairs, the mutual information might  
84 be good only on a small portion of the images. Thus, mutual information  
85 can be used only on a selected region of an image [13], on region with similar  
86 edge density [11], or on a detected foreground [12]. Edges can be used to  
87 obtain a transformation estimate before applying mutual information [14].

## 88 *2.2. Approaches based on features*

89 Edges can be extracted using discrete wavelet transform [15] or Gabor  
90 filters [16]. A threshold is used to select some edges that are considered more  
91 discriminative, and then they are used to compute the transformation matrix  
92 by pairing them in different combination using a RANSAC [4] type method.  
93 The distance between edge points, or invariant moments and contour ori-  
94 entation, are used as the criterion to evaluate a transformation. Another  
95 alternative is to extract the edges with an edge detector, and then group the  
96 edges into segments [17]. Segments are further grouped into triangles. Affine

97 transformation matrices are then computed to align pairs of triangles until  
98 a quality criterion is reached. Similarly, in other works [18, 19], edges are  
99 extracted using the Canny edge detector. The quality of the transformation  
100 is evaluated using the Hausdorff distance between edge points. Finally, edges  
101 and foreground detection may be used [20]. In this case, only the edges on  
102 moving objects are used for computing the registration.

103 Feature point-based methods are founded on the principle that only a few  
104 points with known correspondence are required to compute a registration.  
105 The challenge is to find points that appear both in infrared and visible im-  
106 ages. Corners can be used in some situations, for example, to register facade  
107 [21]. In this case, registration is found by minimizing the Hausdorff distance  
108 between corresponding corners. Another approach is based on foreground  
109 detection and trajectory formed from centroids of the detected blobs [22, 2].  
110 For a given blob, its center of mass (centroid) in consecutive images forms  
111 a trajectory in the video. This method matches points on trajectory pairs  
112 to compute the transformation matrix. Thus, it uses temporal information.  
113 Many combinations of trajectories are tested with a RANSAC algorithm to  
114 minimize the transformation error which is evaluated based on the Euclidean  
115 distance between corresponding trajectory points.

### 116 *2.3. Approaches based on consistent temporal behavior*

117 Alternatively, a third possible approach relies on consistent temporal be-  
118 havior. In intensity and feature based approaches, the image alignment re-  
119 quires a consistent appearance in two images. However, for the alignment of  
120 two image sequences that do have not spatial overlap between their field of  
121 view, retrieving common feature is nearly impossible because the consistent

122 appearance assumption is not valid. Caspi and Irani have proposed a method  
123 for alignment of both in time and space of two image sequences with no over-  
124 lap between their field of view [23]. In their method [23], homography matrix  
125 (2D/3D) between two cameras and temporal synchronization are computed  
126 using the consistency of temporal behavior between two image sequences,  
127 which is satisfied by using two collocated cameras that are moved jointly in  
128 space. In our case, since we have overlapping fields of view, we can use image  
129 features and use a simpler method.

130 Our proposed method is based on the work of [1, 2, 3]. These works  
131 are based solely on the Euclidean distance between corresponding trajectory  
132 points to evaluate candidate transformation matrices. Since trajectories are  
133 essentially one-dimensional, the drawback of this registration criterion is that  
134 it needs many trajectories to restrict the possible transformations between  
135 the two videos. Few trajectories give inaccurate and unstable registration.  
136 In this work, we aim to improve this registration criterion to allow accurate  
137 registration even if only few trajectories are available.

### 138 **3. Methodology**

#### 139 *3.1. Overview of the registration method*

140 Our proposed method is based on trajectories and regions of detected  
141 foreground objects. Figure 1 illustrates the process. The cameras are as-  
142 sumed to be in a stereoscopic configuration, synchronized, and stationary for  
143 the duration of the calibration procedure. We also assume that the objects  
144 are in the same plane, so we can compute the transformation matrix for all  
145 moving objects. The main steps of our method are:

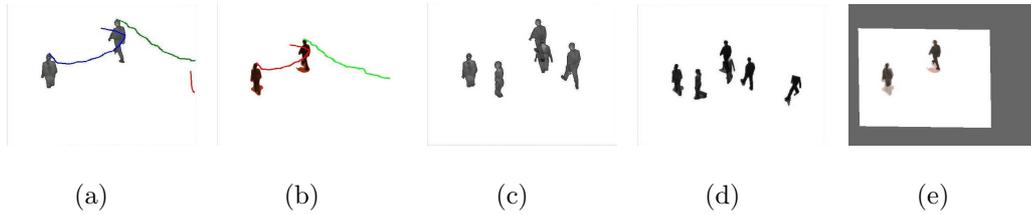


Figure 1: Illustration of processing steps for a given frame. (a) and (b) Object trajectories in IR and visible respectively, (c) and (d) Foreground composite image in IR and visible respectively, (e) Registration result

- 146 1. Find the trajectories of moving objects using a simple tracking method  
147 (figure 1 (a) and (b));
- 148 2. Calculate the new composite foreground images (figure 1 (c) and (d));
- 149 3. Find the best point and trajectory correspondences using a RANSAC-  
150 based method, a transformation matrix, and foreground composite im-  
151 ages;
- 152 4. Calculate the transformation matrix based on the best set of trajectory  
153 points;
- 154 5. Select the best transformation matrix (current versus the new one of  
155 step 4) (figure 1 (e)).

156 In the following, the video sequence of the infrared camera will be referred  
157 to as the left image or the left video. In the same way, the right image or  
158 the right video will correspond to the visible color camera.

### 159 3.2. Background subtraction and tracking

160 In this work, the focus is on the registration method. Thus, background  
161 subtraction and tracking are done using simple methods. Background sub-  
162 traction is performed using the algorithm proposed in [24], which detects

Table 1: Effect of different phenomenon on background subtraction in visible and in infrared

Phenomenon	Is visible affected?	Is IR affected?
Motion in background	Yes (depends on color of moving/moved object)	Yes (depends on temperature of moving/moved object)
Change in lighting	Yes	Only if lighting change is by a significant heat source (e.g. sun)
Change of scene temperature	Only if heat source is emitting light (e.g. sun)	Yes
Cloths with color similar to background components	Yes	No
Cloths at temperature similar to background components	No	Yes
Reflections on polished metal or glass	Only under some lighting conditions or with mirror surfaces	Yes
Shadows of moving objects	Yes	Only if it causes a significant change in temperature (e.g. light emitting heat source is occluded for a long time)

163 the foreground using the temporal average of the color (or intensity) of each  
164 pixel and a threshold. This method is fast but sensitive to lighting (or tem-  
165 perature) variations and it cannot handle periodically changing backgrounds.  
166 Table 1 gives the factors that influences background subtraction in visible and  
167 in infrared. Both infrared and visible are affected by different phenomenon,  
168 but rarely simultaneously, and this is, in fact, why it is useful to use these  
169 two modalities. In our case, the background, the lighting, and the scene tem-  
170 perature do not change significantly, because our method is tested indoor.  
171 Thus, the results are, in general, reliable enough for the following steps.

172 For tracking, we use the method of [25] which is based on the overlap be-

173 tween detected foreground regions in two consecutive frames. This algorithm  
 174 is fast, but it does not handle data associations in complex interactions. The  
 175 tracking results are good enough to test our proposed registration method,  
 176 because it is not concerned with object identities. It only needs trajectories  
 177 of moving foreground regions as input.

178 The result of tracking is a set of trajectories. Trajectories are formed with  
 179 the top pixel coordinates (e.g. top of the head) of all the blobs (connected  
 180 foreground regions) that overlap between two consecutive frames (see figure  
 181 1a and b). Let  $T_{video}^i$  be the  $i^{th}$  trajectory in a given *video* (*right* or *left*).  
 182  $T_{video}^i$  is defined in a matrix form in homogenous coordinates by

$$T_{video}^i = \begin{bmatrix} X_1 & X_2 & \dots & X_n \\ Y_1 & Y_2 & \dots & Y_n \\ 1 & 1 & \dots & 1 \end{bmatrix}, \quad (1)$$

183 where  $n$  is the number of points in the trajectory. Our tracking method  
 184 operates on a set of trajectories at each frame.

### 185 3.3. Registration algorithm

186 To register the infrared and visible videos, we find the trajectory set and  
 187 point set that give the best overlap of an infrared and a visible composite  
 188 foreground image. For each set of trajectories, we compute a transformation  
 189 matrix. The infrared composite foreground image is transformed into the  
 190 referential of the visible composite foreground image using the transformation  
 191 matrix calculated. The overlap between the two images is then calculated,  
 192 and the trajectory set and point set that give the best overlap is selected.  
 193 This results to the final transformation matrix.

194 *3.3.1. Transformation matrix*

195 The goal of registration is to find the transformation matrix  $H$  to convert  
 196 the coordinates of the points of the left video to the referential of the right  
 197 video (i.e. the homography). That is,

$$Coord_{right} = H \times Coord_{left}, \quad (2)$$

198 where  $Coord_{right}$  are the coordinates in the right video referential and  $Coord_{left}$   
 199 are the coordinates in the left video referential. In our case, the cameras are  
 200 fixed on a bar where only translations on the  $X$  and  $Y$  axes are possible  
 201 (see figure 2). Rotations around the  $Z$  axis are also possible. Furthermore,  
 202 the cameras can have different zooms. Because of this setup, the  $H$  matrix  
 203 simplifies to an affine matrix [26].  $H$  is then

$$H = \begin{bmatrix} a_{11} & a_{12} & t_x \\ a_{21} & a_{22} & t_y \\ 0 & 0 & 1 \end{bmatrix}, \quad (3)$$

204 where  $a_{ij}$  are the rotation around  $Z$  and non-isotropic scaling, and  $t_x$  and  
 205  $t_y$  are the translations along  $X$  and  $Y$ , respectively. To find  $H$ , equation  
 206 2 is solved using candidate corresponding trajectory points in the left and  
 207 the right videos, and the normalized Direct Linear Transform (DLT) method  
 208 [26] to find the least square solution because our set of equations is over-  
 209 determined.

210 *3.3.2. Composite foreground images*

211 Two composite foreground images are constructed; one for the left video,  
 212 and another for the right video. This allows our method to perform even if

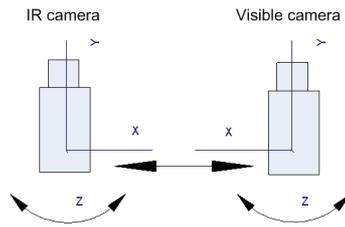


Figure 2: Camera setup

213 there are few trajectories, as regions restrict more the possible transforma-  
 214 tions than a few curves. Furthermore, the use of composite foreground images  
 215 for evaluating the quality of a transformation matrix allows our method to  
 216 produce a transformation matrix for each video frame pair. We get a good  
 217 registration result as soon as we get three corresponding trajectory points in  
 218 both the right and left videos.

219 Each composite image is composed of the superposition of  $F$  binarized  
 220 foreground images (typically  $F = 5$ ). Our goal is to obtain an image with  
 221 foreground blobs localized in the four quadrants of the image. The composite  
 222 image must not be composed of too much blobs because there will be a good  
 223 overlap whichever the transformation matrix as large shapeless regions will  
 224 be obtained. Shape is important to restrict transformations and therefore,  
 225 we need few blobs, but positioned well. A composite foreground image is  
 226 thus composed of the superposition of the current frame plus the last  $F - 1$   
 227 foreground images such that there are blobs in each of the four quadrants  
 228 of the image (if possible). Figure 3 shows composite foreground images for  
 229 a single actor moving in the field of view of the two cameras. It is the  
 230 superposition of four frames.

231 The quality of a transformation matrix is evaluated using as an error

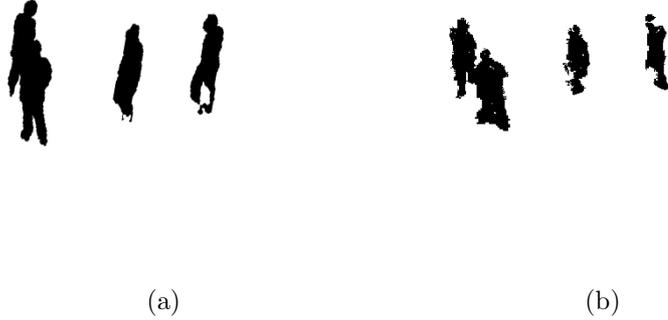


Figure 3: Composite foreground images for a single actor moving in the field of view of IR and visible cameras. (a) Foreground composite image for IR camera, (b) Foreground composite image for visible camera.

function the overlap error  $OE$  of the two composite foreground images with

$$OE = 1 - \frac{N_{left \cap right}}{N_{left \cup right}}, \quad (4)$$

where  $N_{left \cap right}$  is the number of overlapping foreground pixels and  $N_{left \cup right}$  is the number of foreground pixels from the union of the right image and left image.

We have chosen to build a composite foreground image to verify transformations instead of combining transformation results from many individual foreground images, because we wish to obtain a transformation matrix that can explain the image globally to obtain a unique and stable registration matrix. That is, we are assuming that all image areas include valuable information. A given individual foreground image may give a good transformation matrix only over a small image area since the known information about the whole image is small and the transformation degrees of freedom are not restricted enough (many matrices can explain the transformation of

245 the small known area). The composite foreground images resolve the dif-  
246 ficulty of merging disparate transformation matrices, and aim at obtaining  
247 information across the image to restrict the possible transformations.

### 248 3.3.3. Finding the best set of trajectory points

249 For registration, we find the correspondence between the different trajec-  
250 tories. A RANSAC-based algorithm is used. It has the following steps:

251 *Repeat 1. - 4. until error is sufficiently small*

252 1. Pick a trajectory pair at random

253 *Repeat (a) -(e) until error is sufficiently small*

254 (a) Pick three pairs of points at random in the selected trajectory pair

255 (b) Calculate H (equation 2)

256 (c) Add participating point pairs

257 (d) Recalculate H (equation 2)

258 (e) Evaluate overlap error using Euclidean distance

259 2. Add participating trajectory pairs

260 3. Recalculate H (equation 2)

261 4. Evaluate overlap error using equation 4

262 First, a set of all possible corresponding trajectory pairs is constructed.  
263 A pair is formed from two trajectories, one from the left video and the other  
264 from the right video. Each iteration, a trajectory pair is picked at random  
265 using the RANSAC method and a transformation matrix is calculated us-  
266 ing corresponding points. Since the videos are synchronized, corresponding  
267 points in a trajectory pair are points that have the same timestamp. There  
268 are often more than three possible pairs of points in a trajectory pair. Some

269 pairs are inliers, and others are outliers because of tracking errors or top of  
270 the head position errors caused by the foreground extraction. That is, trajec-  
271 tories might match only partially because of tracking errors and as a result,  
272 all point pairs should not be considered. Thus, three pairs of corresponding  
273 points are picked at random using, again, the RANSAC method. The Eu-  
274 clidean distance between left transformed points (using  $H$  calculated with  
275 equation 2) and there corresponding points in the right video are computed.  
276 Pair of points for which the Euclidean distance is smaller than a threshold  $t$   
277 (typically,  $t = 5$  pixels) are considered as participating point pairs.

278 The selection of random point pairs for a given trajectory pair is repeated  
279 until the error is sufficiently small in the RANSAC algorithm. We use a  
280 confidence  $p$  of 0.99.

281 For the selection of the random trajectory pairs, the same principle is  
282 used, but the participating trajectory pairs are established using the com-  
283 posite foreground images. For a given trajectory pair, the quality of the  
284 transformation is evaluated using equation 4. A participating trajectory pair  
285 is a trajectory pair, which decreases the overlap error (value of equation 4).

286 To summarize our selection of the best corresponding trajectory points,  
287 we first use a RANSAC algorithm to select trajectory pairs at random using  
288 the composite foreground images to evaluate the quality of  $H$ . We use a  
289 second RANSAC algorithm to select at random, point pairs inside a given  
290 trajectory pair using the Euclidean distance as the criterion for evaluating  $H$ .  
291 This process results in selecting the best corresponding trajectories and the  
292 best corresponding points within corresponding trajectories. The selected  
293 points are then used to calculated  $H$ .

### 294 3.4. Selection of the best transformation matrix

295 The principle of our method is that the estimation of the affine matrix  
296  $H$  should improve as points are added to the trajectories. Thus, earlier  
297 estimation should be replaced with a newer if it decreases the overlap error of  
298 the composite foreground images. For each frame, equation 4 is computed for  
299 the previous  $H$  and the new estimation. If overlap relative error  $E$  increases  
300 with the new estimation, the previous  $H$  is kept, if not, it is replaced with  
301 the new estimation.

## 302 4. Experiments

### 303 4.1. Experimental methodology

#### 304 4.1.1. Data acquisition and setup

305 For all experiments, a FLIR Thermovision A40 camera (infrared) and  
306 a Sony DFW-SX910 camera (color) were used. Videos are 320x240@7,5fps.  
307 The cameras were supported by one or two tripods depending on the baseline  
308 distance. On the same tripod, the cameras were distanced by 19 cm and on  
309 two tripods by approximately 80 cm. All scenarios were filmed from the  
310 top to obtain trajectories that are not too linear<sup>1</sup> and in the same plane.  
311 Scenarios involve one or more actors (between 1 and 5) and different baseline  
312 (19 cm or approximately 80 cm).

#### 313 4.1.2. Comparison with previous method

314 In our method, the transformation matrix for each frame is found by  
315 minimizing equation 4, that is the overlap between composite foreground

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<sup>1</sup>To compute the affine matrix, the three points in each image must not be collinear.

316 images. To compare our proposed error function with previous work, we  
317 compared our method with the method of [2] in which the error function is the  
318 Euclidean distance between the right trajectory points and the transformed  
319 left trajectory points. For comparing our error function with theirs, we made  
320 a second version of our method which uses this error function instead of ours.  
321 This allows us to assess the benefit of our proposed error function. For all  
322 results, we show the performance using our proposed error function and the  
323 Euclidean error function.

#### 324 *4.1.3. Ground-truth and evaluation metrics*

325 To quantify registration errors, it is necessary to measure the pixel dis-  
326 placement error between the left image and the transformed right image. To  
327 do this, some kind of ground-truth and a metric is needed. As ground-truth,  
328 we have introduced in the scene for all videos cold square cardboards, visible  
329 both in infrared and in color images (see figure 4). Square cardboards were  
330 cooled down outdoor at a temperature of  $-20^{\circ}C$  during a few minutes. The  
331 cardboards in infrared are visible only at the beginning of the video when  
332 the scene is empty of moving objects, so for both visible and infrared, the  
333 cardboards are part of the background model of the scene during processing.  
334 Ground-truth binary images were constructed by a human operator selecting  
335 manually the corner points of cardboards in the left and right image. Since  
336 ground-truths do not move and are part of the scene to be registered, this can  
337 be done for only one pair of images. A good transformation matrix should  
338 allow overlapping the cardboard areas with small displacement error. The  
339 displacement error can be measured either by calculating the maximum dis-  
340 placement of the cardboard corners points or by verifying the overlap error.

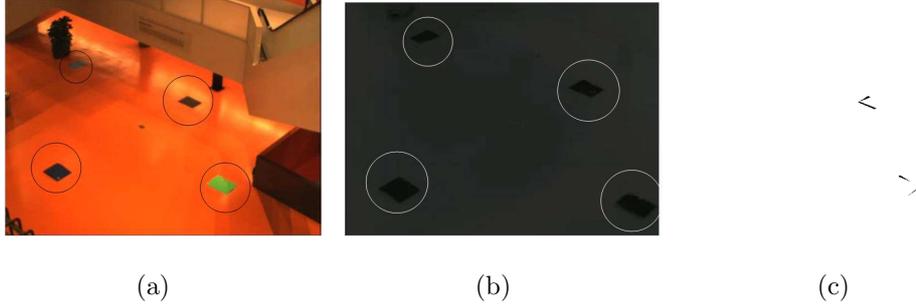


Figure 4: Cold square cardboards used for ground-truth. (a) Cardboards in color image, (b) Cardboards in infrared image, (c) An overlap error of the cardboards of 16.5% ( $E = 0.165$ ).

341 We have chosen to calculate the overlap error as the implementation of our  
 342 method has already the functionality for such a task.

343 The overlap error  $E$  is calculated as follows:

- 344 1. Create ground-truth by selecting the corners of the cardboards for a  
 345 test video. This gives two binary images of the cardboards in the visible  
 346 and infrared ( $CB_{left}$  and  $CB_{right}$ ) that are used at each frame to verify  
 347 the quality of registration;
- 348 2. Process each frame  $f$  of the same test video. Apply our method to  
 349 find transformation matrix for frame  $f$  using proposed (composite fore-  
 350 ground images) or Euclidean error function.
- 351 3. Register the two cardboard binary images using the transformation  
 352 matrix obtained.
- 353 4. Compute the overlap error with:

$$E = 1 - \frac{P_{CB_{left} \cap CB_{right}}}{P_{CB_{left} \cup CB_{right}}}, \quad (5)$$

354 where  $P_{CB_{left} \cap CB_{right}}$  is the number of overlapping ground-truth card-  
 355 board pixels and  $P_{CB_{left} \cup CB_{right}}$  is the number of ground-truth card-

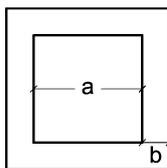


Figure 5: Typical displacement and overlap error geometry.

356 board pixels from the union of the cardboards binary images ( $CB_{left}$   
 357 and  $CB_{right}$ ).

358 Note that the cardboards are not part of the foreground in the videos,  
 359 and thus they are not used to find the transformation matrix with our pro-  
 360 posed method. Our proposed error function minimizes the overlap error of  
 361 composite foreground images, not the overlap of the cardboards. As such,  
 362 our method is not favoured even though the evaluation metric has the same  
 363 formulation as the proposed error function. Also, we do the transformation  
 364 matrix computations continuously for evaluation purposes, but could be stop  
 365 after a given number of frames.

366 Relative mean displacement error  $b$  is related to our relative overlap error  
 367  $E$  approximately in the following way (see figure 5):

$$E = 1 - \frac{a^2}{(a + 2b)^2} \quad (6)$$

$$368 \quad E(a + 2b)^2 = (a + 2b)^2 - a^2 \quad (7)$$

$$369 \quad a = \sqrt{(a + 2b)^2 - E(a + 2b)^2} \quad (8)$$

$$370 \quad (a + 2b) - 2b = \sqrt{(a + 2b)^2 - E(a + 2b)^2} \quad (9)$$

371 Since  $a + 2b = 1$ ,

$$1 - 2b = \sqrt{1 - E} \quad (10)$$

372 And thus,

$$b = \frac{1 - \sqrt{1 - E}}{2} \quad (11)$$

373 From equation 11, it means that for an overlap error  $E = 0.1(10\%)$ , we  
374 obtain a relative mean displacement error of  $b=0.026$ . Thus, for an average  
375 cardboard size of 25 pixels, the absolute mean displacement error is about  
376 0.6 pixel ( $b \times 25$ ). For  $E = 0.2$ , it is about 1.3 pixels, for  $E = 0.3$ , it is about  
377 2 pixels, and for  $E = 0.4$  it is about 2.8 pixels.

378 Furthermore, we have compared the automatic registration results with  
379 manual registration. The ground-truth affine transformation matrix was cal-  
380 culated from the corners points of the cardboards using equation 2. The error  
381  $E$  (equation 5) is also calculated for the cardboards to be used as a reference.  
382 This is what we consider the ground-truth error. It is not necessarily zero,  
383 because the points are selected manually (see figure 4(c)). Furthermore, to  
384 verify the overlap of the cardboards and to compute  $E$ , we have to cut them  
385 out manually from the color and infrared images and in general, they are not  
386 cut out perfectly as the boundaries are not always sharp.

387 Since RANSAC is not a deterministic algorithm, to have statistically  
388 sound results, each experiment was repeated 30 times [27]. Our results are  
389 statistics over these repetitions, and they are the mean, minimum, median  
390 and standard deviation ( $\sigma$ ) of  $E$  for the 30 repetitions at each frame. To  
391 synthesize the results, we show in the tables, the mean of three statistical  
392 measures (mean, minimum and  $\sigma$ ) at each frame for the complete videos.  
393 That is for a frame, we calculate the mean overlap error  $E$  (out of 30 repe-  
394 titions), and for a test scenario, we do the mean of the means of each frame.  
395 The mean of the means ( $\mu_{\bar{E}}$ ) is given by

$$\mu_{\bar{E}} = \frac{\sum_{j=1}^{NF} \frac{\sum_{i=1}^{30} E_i^j}{30}}{NF}, \quad (12)$$

396 where  $E_i^j$  is the overlap error of a repetition  $i$  of RANSAC for the  $j$ th  
 397 frame, and  $NF$  is the number of frames in the test video. We did the same  
 398 for the minimum and  $\sigma$  (mean of the minimums ( $\mu_{min}$ ) and mean of  $\sigma$  ( $\mu_{\sigma}$ )).

#### 399 4.2. Results and discussion

400 Table 2 gives the mean of the minimums ( $\mu_{min}$ ) for each scenario. It  
 401 shows that the use of the composite foreground images allows us to obtain  
 402 results that are consistently closer to the ground-truth compared to the use of  
 403 only Euclidean distance between trajectory points. Thus, the use of blobs as  
 404 a quality criterion to evaluate a transformation matrix stabilizes the results.  
 405 Figure 6 shows the complete results for scenario 3. This figure shows that  
 406 the mean and  $\sigma$  change a lot at every frames when using only the Euclidean  
 407 error function. Furthermore, we get better results faster (within 130 frames  
 408 for 30% error compared to around 170 frames). The foreground composite  
 409 images restrict significantly more the number of possible transformations.  
 410 Thus, we believe the use of this strategy is an important contribution to a  
 411 feature point-based method.

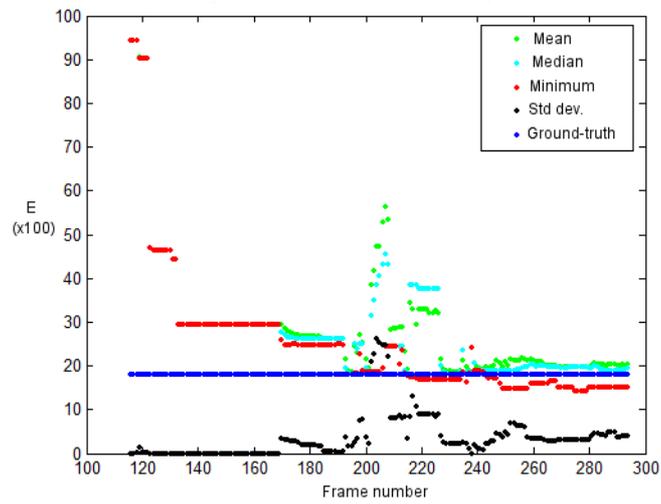
412 The reader can notice an increase in  $\sigma$  between frames 200 and 220 (fig-  
 413 ure 6). In this interval, there are many background subtraction errors, and  
 414 the transformation between the two videos becomes harder to establish. In  
 415 fact, in this interval, the foreground is not well detected, and there are less  
 416 foreground pixels in the visible composite image which makes the overlap

Table 2: Results for nine scenarios (mean of the minimums ( $\mu_{min}$ ) at each frame)

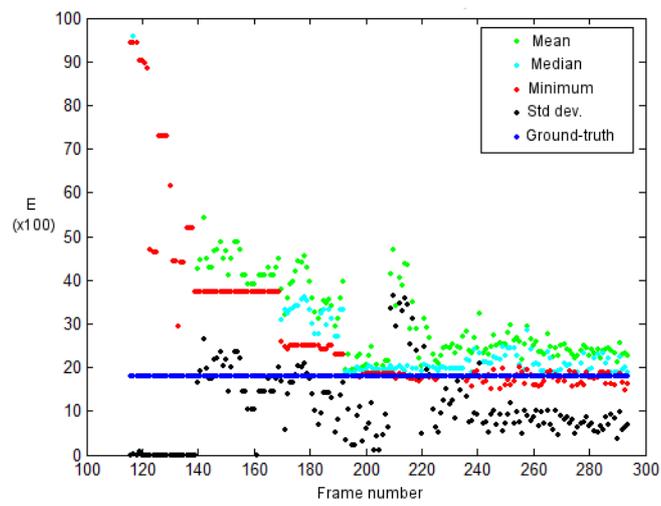
Scenario	Ground-truth	Proposed error function	Euclidean error function
1	0.210	<b>0.267</b>	0.323
2	0.205	0.403	<b>0.395</b>
3	0.178	<b>0.251</b>	0.280
4	0.183	<b>0.184</b>	0.300
5	0.165	<b>0.407</b>	0.541
6	0.119	<b>0.221</b>	0.253
7	0.112	0.152	<b>0.139</b>
8	0.274	<b>0.264</b>	0.334
9	0.123	<b>0.085</b>	0.112

417 more ambiguous. Since the selection of the transformation matrix relies on  
 418  $OE$  (see 3.4), we may select a less accurate matrix (w.r.t. ground-truth and  
 419  $E$ ) than the previous one. To solve this, we could make statistics on the best  
 420 transformation matrices found at every frame, and select a matrix that min-  
 421 imizes  $OE$  for many frame. We could also build the transformation matrix  
 422 from the matrices of many frames.

423 Sometimes our algorithm gets results with error  $E$  smaller than the  
 424 ground-truth. It is possible and desirable because the cardboards are not  
 425 cut out perfectly and the ground-truth is selected by hand, so there is a mar-  
 426 gin of error and we expect automatic registration to be more precise than a  
 427 manual one. It is possible that we did not select accurately the corners of  
 428 the cardboards. Notice that the Euclidean error method can also give results



(a)



(b)

Figure 6: Results for scenario 3. (a) Proposed error function, (b) Euclidean error function.

429 better than the ground-truth. For the mean of the minimums ( $\mu_{min}$ ), our  
430 method is outperform slightly two times by the Euclidean error method.

431 If we now consider table 3, our method gives in general mean transfor-  
432 mation matrices that are closer to the ground-truth. It is not the case for  
433 scenario 2 and 7. For the second scenario, the results are about the same,  
434 but for scenario 7, our method is significantly outperformed. Figure 7 details  
435 the result. Our method is still more stable compared to the Euclidean error  
436 method, but the transformation error stays large. This test scenario involves  
437 five actors and as a result much more trajectories. In this case, the Eu-  
438 clidean error method can find better results. In fact, this method is design  
439 to perform well with many trajectories, while our method aims at solving  
440 the case where they are fewer trajectories. For this scenario, the composite  
441 foreground images become very crowded, and a bad transformation (w.r.t.  
442 ground-truth) can give a good overlap. To solve this, we should verify that  
443 the foreground blobs in the composite foreground images do not cover an  
444 area that is too large, and in such case, consider fewer frames to superpose  
445 in the composite foreground images.

446 The two methods do not work as well when the baseline is larger (scenario  
447 5), because there is less overlap between the two images. Thus, there are more  
448 ambiguities and fewer points to pair.

449 Finally, table 4 gives the mean of the standard deviations ( $\mu_{\sigma}$ ) for each  
450 frames. Except for scenario 7, for the reasons previously explained, our  
451 method outperforms the Euclidean error method. If not, the results are  
452 about the same.

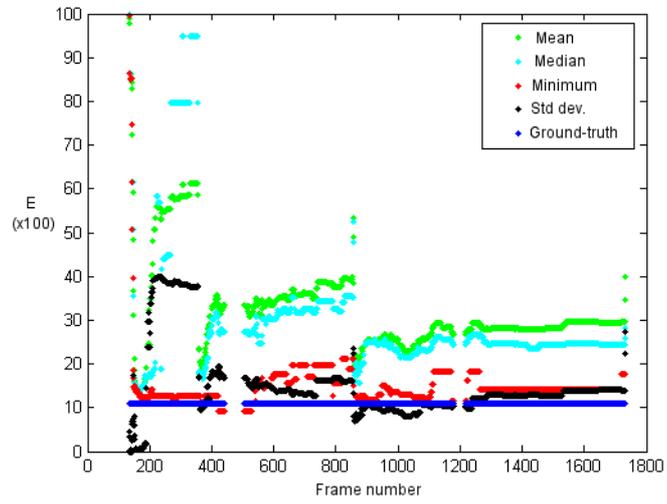
453 Figure 8 shows actual registration results obtained for frame 48 of scenario

Table 3: Results for nine scenarios (mean of the mean ( $\mu_{\bar{E}}$ ) at each frame)

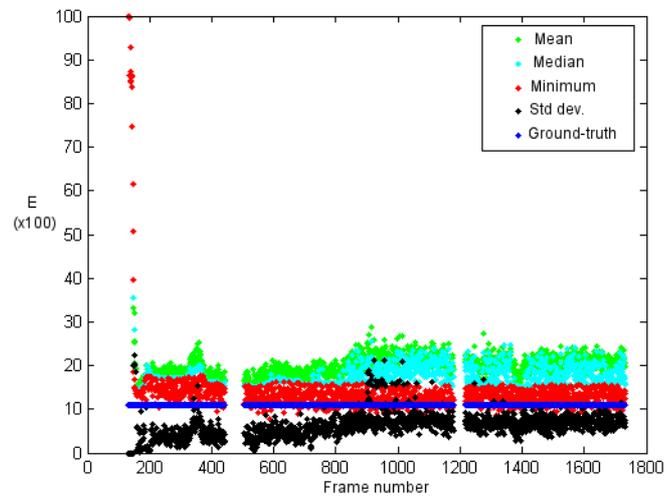
Scenario	Ground-truth	Proposed error function	Euclidean error function
1	0.210	<b>0.329</b>	0.601
2	0.205	0.419	<b>0.416</b>
3	0.178	<b>0.294</b>	0.351
4	0.183	<b>0.270</b>	0.350
5	0.165	<b>0.522</b>	0.700
6	0.119	<b>0.284</b>	0.302
7	0.112	0.328	<b>0.206</b>
8	0.274	<b>0.348</b>	0.404
9	0.123	<b>0.177</b>	0.201

Table 4: Results for nine scenarios (mean of  $\sigma$  ( $\mu_{\sigma}$ ) at each frame)

Scenario	Ground-truth	Proposed error function	Euclidean error function
1	0	<b>0.064</b>	0.116
2	0	0.021	<b>0.012</b>
3	0	<b>0.035</b>	0.109
4	0	0.065	<b>0.055</b>
5	0	<b>0.060</b>	0.072
6	0	<b>0.057</b>	0.058
7	0	0.152	<b>0.062</b>
8	0	0.082	<b>0.075</b>
9	0	<b>0.085</b>	0.113



(a)



(b)

Figure 7: Results for scenario 7. (a) Proposed error function, (b) Euclidean error function.

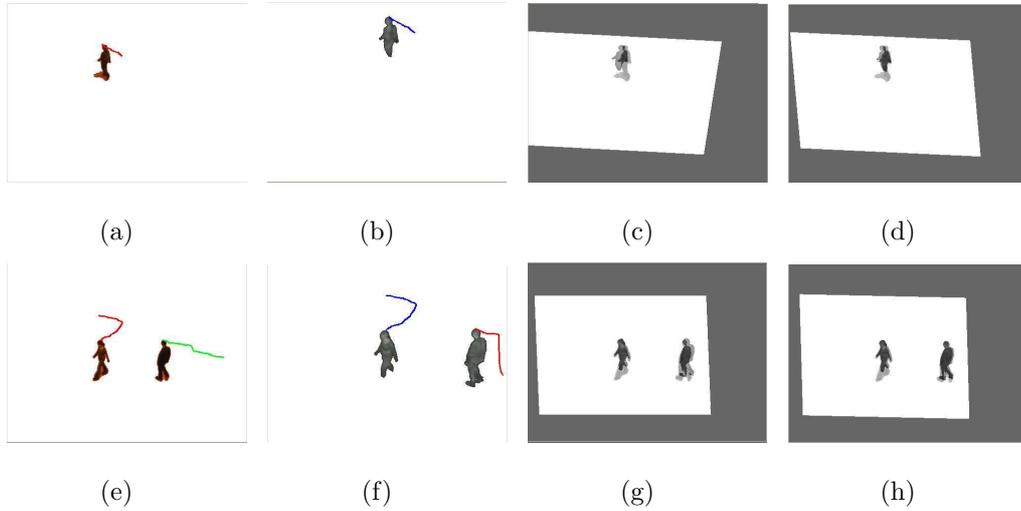


Figure 8: Registration results for two pairs of frames. (a) to (d), frame 48 from scenario 1: (a) Visible image and computed trajectory, (b) IR image and computed trajectory, (c) Registration of (a) and (b) with Euclidean error function, (d) Registration of (a) and (b) with our proposed error function. (e) to (h), frame 98 from scenario 9: (e) Visible image and computed trajectories, (f) IR image and computed trajectories, (g) Registration of (e) and (f) with Euclidean error function, (h) Registration of (e) and (f) with our proposed error function.

454 1 and for frame 98 of scenario 9. In the first case (Figure 8 a,b,c,d), because of  
 455 the small number of trajectory points, the transformation matrix found using  
 456 Euclidean error function does not give a good registration. Conversely, using  
 457 our proposed error function allows a better registration because the region  
 458 overlap constrains more the set of possible transformations. In the second  
 459 case (Figure 8 e,f,g,h), the registration is again better with our proposed  
 460 error function, because even if more trajectory points are available, their  
 461 positioning might not be exact, and thus transformations are less constrained  
 462 than with a region.

463 *4.3. General discussion*

464 Globally, the use of the composite foreground images allows our method  
465 to perform better when there are fewer trajectories compared to the use of  
466 Euclidean distance on trajectory points. Furthermore, it stabilizes the trans-  
467 formation matrix obtained and the RANSAC algorithm gives more consis-  
468 tently the same result. This is because we are registering information across  
469 the whole image, and thus the possible transformations are more restricted.  
470 However, when there are more actors, our composite foreground images might  
471 get too crowded. In this case, it should be composed of less frames (i.e.  $F$   
472 should be smaller than 5).

473 The core of our method, our proposed overlap error function, is not re-  
474 stricted to affine transformation, as any registration, whichever the 2D ho-  
475 mography matrix used, should overlap images almost perfectly. Thus, the  
476 goal of having a good level of overlap everywhere in an image is valid for any  
477 2D homography matrix. Our method could be applied for projective 2D ho-  
478 mography by just changing matrix calculation. If the matrix is not changed,  
479 the overlap will not be as good, but since in the composite foreground images  
480 there should be objects all across their areas, the overlap criterion will still  
481 restrict as much as possible the possible transformations as desired.

482 Synchronization may affect the results because synchronization error will  
483 cause different or displaced shapes to be overlapped. In this work, we assume  
484 that the cameras are synchronized. Actually, since they are synchronized by  
485 software, images from both cameras are obtained sequentially, and the frame  
486 rate is relatively low, images are in fact not perfectly synchronized (see for  
487 example figure 1a) and b), the spacing between the legs of the right actor is

488 different). The desynchronization of the legs does not affect too much the  
489 result because it corresponds to small areas. However, the positional error for  
490 large desynchronization will cause more problems. Fortunately, the videos  
491 may be synchronized by the method proposed by [2]. Applying this method  
492 would have reduced the errors we have calculated in our experiments for the  
493 two methods, but with similar conclusions.

494 Object detection also affects the results. The top of the head position  
495 might change and the areas to overlap will have different shapes. By using  
496 composite foreground images, local background subtraction errors will not  
497 cause significant overlap errors since the total area to overlap is large. Back-  
498 ground subtraction errors will cause difficulties only if they affect a large  
499 part of the image during many frames, because our foreground composite  
500 images include frames at different moment in time. The trajectories may be  
501 significantly affected too by background subtraction errors. Some trajectory  
502 points will be incorrectly positioned. They will be rejected based on our error  
503 function since they will not produce good overlap of foreground composite  
504 images. In fact, trajectories and object regions will be affected independently  
505 in general since we use the top of the head for trajectories. For example, if  
506 the head of a human is missing, there will be an error in the trajectory but  
507 the body region to overlap will be large and almost complete. Whereas if  
508 only the head is detected, the trajectory will be good, but there will be a  
509 large overlap error for this human.

## 510 5. Conclusion

511 In this paper, we presented a method and a novel criterion to register  
512 infrared and color (visible) videos. It is a feature point-based method that  
513 uses top pixel coordinates found after foreground detection and tracking to  
514 build trajectories in both visible and infrared videos. Then, the trajectory  
515 points are used to find the transformation matrix that is obtained using a  
516 RANSAC algorithm and composite foreground images as quality criterion.

517 The results obtained show that the use of composite foreground images  
518 as a registration criterion give results that are more stable compared to a  
519 criterion on trajectories. Furthermore, it allows working with video in which  
520 there are few trajectories. In general, the results are close to the ground-  
521 truth. Because our proposed method aligns silhouettes instead of trajectory  
522 points, it is appropriate for method performing image fusion using blob con-  
523 tours or edges.

524 Future works are to improve the construction of the foreground composite  
525 image to ensure that it is not too crowded, which reduces its benefit, and to  
526 test the method with a more sophisticated tracking method to obtain better  
527 trajectory points. We should also design a method to assess the quality of the  
528 foreground detection. Registration could be performed only when foreground  
529 detection is acceptable. In addition, the selection of the best transformation  
530 matrix for the complete video should be improved as noted in the discussion.

531 We also aim at integrating this method with tracking to design a day/night  
532 tracking system that combines information from both infrared and visible  
533 sensors using a feedback between tracking and registration.

534 **6. acknowledgements**

535 We would like to thank the Canadian Foundation for Innovation (CFI)  
536 and the Fonds québécois de la recherche sur la nature et les technologies  
537 (FQRNT) for their support with grants.

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