

An iterative integrated framework for thermal-visible image registration, sensor fusion, and people tracking for video surveillance applications

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Abstract

In this work, we propose a new integrated framework that addresses the problems of thermal-visible video registration, sensor fusion, and people tracking for far-range videos. The video registration is based on a RANSAC trajectory-to-trajectory matching, which estimates an affine transformation matrix that maximizes the overlapping of thermal and visible foreground pixels. Sensor fusion uses the aligned images to compute sum-rule silhouettes, and then constructs thermal-visible object models. Finally, multiple object tracking uses blobs constructed in sensor fusion to output the trajectories. Results demonstrate the advantage of our proposed framework in obtaining better results for both image registration and tracking than separate image registration and tracking methods.

Key words: Thermal camera, visible camera, thermal-visible image registration, sensor fusion, multiple people tracking

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1. Introduction

In the recent years, there has been a growing interest in visual surveillance using multimodal sensors, such as thermal and visible cameras in both civilian and military applications. Zhu and Huang give a comprehensive introduction about multimodal surveillance systems in [1]. The advantages of jointly using a thermal camera and a visible camera have been studied and discussed extensively in some few works such as [1, 2]. Two main benefits of the joint use of thermal and visible sensors are first the complementary nature of different modalities that provides the thermal and color information of the scene and second, the redundancy of information captured by the different modalities, which increases the reliability and robustness of a surveillance system. These advantages motivated the computer vision community to study and investigate algorithms for thermal-visible video surveillance systems.

For approximately planar far-range videos at different zoom settings, where extracting low level features inside ROIs are difficult due the small size of objects, using the spatio-temporal information of the scene, such as object trajectories and performing sequence-to-sequence matching rather than low level image-to-image matching is an interesting solution. In Caspi *et al.*, a feature-based video sequence-to-sequence matching technique is proposed based on matching object trajectory points [3]. However, trajectory-based matching involves another problem, which is computing trajectories of moving objects in the scene for a pair of video sequences. Since the features to match are trajectory points, the accuracy of computed trajectories in both thermal and visible video has a crucial effect on the image registration result.

In our previous work [4, 5], we proposed trajectory-based sequence-to-sequence

26 video registration, where the object trajectories were computed separately offline
27 for thermal and color video sequences using multiple object tracking, but with an
28 improved trajectory matching that uses foreground pixel overlapping as well as
29 trajectory point matching as registration criteria. In [4, 5], the image registration
30 is similar to the one we used in this paper; however, since the trajectories were es-
31 timated separately from tracking using data of a single modality, some trajectories
32 (registration input data) were inaccurate and disconnected. Furthermore, the fore-
33 ground pixel overlapping criterion could be misleading for some video frames due
34 to the background subtraction errors. In this paper, we address the problem of im-
35 age registration and object tracking in a novel integrated framework with the final
36 goal of improving both registration and tracking. We propose an iterative, inte-
37 grated, thermal-visible video registration, sensor fusion, and multimodal tracking
38 for two synchronized streams of long-range videos recorded by collocated visible
39 and thermal cameras at different zoom settings. For our proposed methods, no
40 camera calibration is needed. The only assumption is the intersection of field of
41 view between thermal and visible cameras. In this paper, we mainly focus on a
42 feedback scheme and collaboration between the three modules of our system (im-
43 age registration, sensor fusion, and tracking), but we also suggest a fusion score
44 computed in the sensor fusion module of our system as an improved registration
45 criterion.

46 **Contribution.** Our proposed integrated framework improves both registra-
47 tion and tracking by providing better quality for their input data. Thermal-visible
48 sensor fusion improves the input data for tracking in thermal and visible videos,
49 which results in more accurate object trajectories. Using accurate trajectories as
50 registration input data results in more accurate image registration. In our experi-

51 ments, we show that our proposed framework outperforms similar image registra-
52 tion methods previously proposed in the-state-of-the-art [3, 5]. Also, we propose a
53 new transformation matrix selection method based on the fusion scores computed
54 in our sensor fusion step. The algorithms presented in this manuscript are based
55 on [6], but they are further developed with detailed analysis and new evaluations.

56 In the remainder of this paper, we present some background (section 2), then
57 the architecture of the whole system (section 3), followed by a description of our
58 image registration, sensor fusion, and tracking (sections 4, 5, and 6). Then, we
59 discuss the performance of our proposed method (section 7). Finally, we conclude
60 our paper (section 8).

61 **2. Related works**

62 Despite the advantages of multimodal surveillance systems, jointly using two
63 sensors of different modalities increases the complexity of a surveillance system
64 and raises new problems such as image registration and multimodal data fusion.
65 Several works are related to algorithms for thermal-visible data fusion. Conaire
66 *et al.* compared the various fusion methods by evaluating the tracking perfor-
67 mance of systems using different fusion methods for aligned pairs of images [7].
68 Their image alignment is done by estimating the optimum planar homography us-
69 ing a manual process and then warping the thermal images. Also Sadjadi gave a
70 comparative analysis of various fusion methods by proposing a set of measures
71 to study directly their performance [8]. Furthermore, Conaire *et al.* proposed a
72 framework that performs data fusion and tracking in one integrated system [9]. In
73 their framework, data fusion is based on fusing the output of multiple spatiogram
74 trackers. In another work, Kumar *et al.* proposed a multimodal object detection

75 based on fusion of blobs in thermal and visible foreground images [10]. Their
76 method addresses the problem of uncertainty in object detection for dynamic en-
77 vironment such as outdoor scenes. Their fusion method is based on a feedback
78 scheme that performs a simple blob matching between fuse blobs in the previous
79 frame and blobs detected individually in the current thermal and visible frames,
80 followed by a belief fusion that determines the validity of foreground regions de-
81 tected for each modality and a Kalman filter fusion method. However, in their
82 method, they did not address the problem of object tracking (tracking is based on
83 a simple blob matching) and image registration.

84 Moreover, a number of works have been published on computer vision meth-
85 ods appropriate for thermal-visible video surveillance applications including back-
86 ground subtraction, object detection [11, 12], multi-pedestrian tracking, and clas-
87 sification [13, 14, 9, 15]. In the works mentioned above, especially the ones de-
88 signed for approximately planar far-range scenes [10, 9], the problem of automatic
89 video registration is not studied. However, in thermal-visible video surveillance
90 applications, where the thermal and visible videos are captured by two synchro-
91 nized cameras with different lenses or zooms and with different FOVs, the primary
92 problem before data fusion or any further analyses is automatic image registration.
93 Due to the numerous differences in imaging characteristics of thermal and visible
94 cameras, finding appropriate correspondence measure for matching multimodal
95 images is challenging. Most methods used for registering images of single imag-
96 ing modality are not applicable. It is also very difficult to find correspondence for
97 an entire scene.

98 In the literature, some works have been proposed on multimodal image reg-
99 istration for various computer vision applications. Krotosky and Trivedi give a

100 comparative analysis of multimodal image registration methods [16]. Most of
101 these works address the image registration problem as a low-level image-to-image
102 feature-based matching problem. In this approach, image features are first ex-
103 tracted and then a matching is done between the dense or sparse extracted fea-
104 tures of a pair of images. For example, Irani *et al.* proposed an image registration
105 method by which local correlation values of the features extracted from a Gaus-
106 sian pyramid of visible and thermal images are computed, and a global align-
107 ment using an iterative Newtonian method is performed [17]. In Coiras *et al.*,
108 image registration is estimated from an affine transformation that maximizes the
109 global edge-formed triangle matching [18]. In Han *et al.*, a hierarchical genetic
110 algorithm-based method is applied for matching the human silhouette in thermal
111 and visible images using two pairs of corresponding points of a human walking
112 on a straight line at a fixed distance from the camera [19]. In these methods, the
113 quality of image alignment is limited to the quality of low-level image feature
114 extraction. Especially for far-range scene people monitoring, extracting features
115 inside blobs is more difficult because blobs are small. Therefore, low-level fea-
116 ture extraction is quite problematic. The other image-to-image matching approach
117 for thermal-visible image registration is the dense stereo correspondence method
118 which is basically a scanline- search box matching followed by a dense disparity
119 map estimation based on the winner takes all (WTA) approach. For example, in
120 Krotosky and Trivedi work, a mutual information (MI) based image registration
121 method is proposed for calibrated pair of thermal and visible images in a close
122 range scene [16]. The robustness of this method is limited by MI window sizes
123 that are needed to be large enough to sufficiently populate the joint probability
124 histogram of MI computation. For far-range people monitoring applications, this

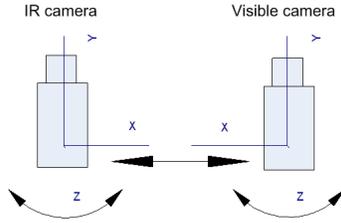


Figure 1: Camera setup

125 assumption is usually not satisfied due to the small size of blobs and lack of de-
 126 tails of patterns inside blobs. Moreover, a simpler camera setup that does not need
 127 further pre-processing such as multimodal calibration is desirable.

128 3. Overview of methods

129 The input data of the system are synchronized video streams captured by a
 130 thermal and a visible camera that are collocated with intersecting fields of view
 131 (FOVs) at different zoom settings. We assume that the scene is planar, which
 132 means that difference of the distances of moving objects in the scene are much
 133 smaller than the distance of the scene from the camera. Fig. 1 shows the camera
 134 setup. Cameras can rotate around the z -axis and move along the x -axis and y -axis
 135 relative to each other. The only requirement is the intersection of fields of view of
 136 the two cameras.

137 The input data of our system at each frame are pair of thermal and visible
 138 foreground images. We apply the background subtraction background method
 139 proposed by [20] to separate the foreground pixels from the background. Any
 140 reasonable background subtraction method with a fair number of false negative
 141 and false positive foreground pixels may be used. Fig. 2 shows the flowchart of
 142 our algorithm, which consists of two stages: 1) initialization; and 2) the main loop

143 for image registration, sensor fusion, and tracking. Initialization is performed at
144 the beginning of the videos, where, for some frames, tracking is performed sepa-
145 rately for the thermal and the visible video frames until we obtain enough object
146 trajectory points in the scene to estimate a good transformation matrix. The sec-
147 ond part of the algorithm consists of a loop on pairs of thermal and visible video
148 frames, where image registration, sensor fusion, and thermal-visible tracking are
149 performed respectively. The image registration estimates an affine transformation
150 matrix, which is used to transform one image into the coordinates of the second
151 one. The sensor fusion matches the color and thermal pixels of blobs using this
152 transformation matrix, and combines thermal and color information. At this step,
153 the matching quality of the computed blobs is also evaluated to decide whether a
154 new transformation matrix should be estimated or if it should be skipped at the
155 next frame. Finally, tracking is performed for thermal and visible videos using
156 fuse blobs obtained from the sensor fusion. These new trajectory points will be
157 used for image registration computation at the next frame.

158 **4. Thermal-visible image registration**

159 At the beginning of the videos, a few trajectory points that are not collinear
160 are required to compute a reasonable initial estimate of the transformation matrix
161 that will be used for sensor fusion. For a fixed number of frames, tracking is
162 performed separately in thermal and visible videos. Then, videos are registered
163 and the overlapping error (Eq. 3) is computed. The registration is repeated until
164 reaching a frame for which the overlapping error is less than a fixed threshold, to
165 ensure the acceptable quality of image alignment required for sensor fusion. The
166 number of initialization frames is subject to change from one video sequence to

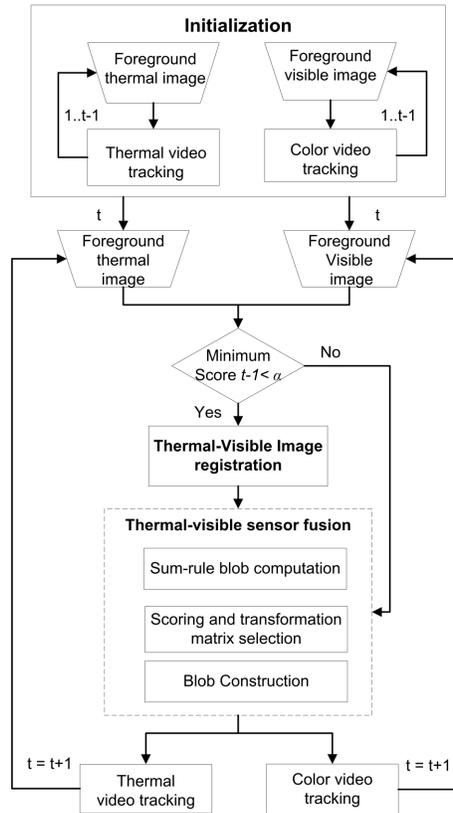


Figure 2: Flowchart of our system

167 another, based on the frame rate of the video, the trajectory pattern of the moving
168 objects in the scene, and the number of the people walking in the FOV of the
169 cameras at the beginning of the video.

170 Image registration is performed by aligning the thermal and color images us-
171 ing an affine transformation matrix H [21] computed by matching object trajectory
172 pairs and point pairs from thermal and visible videos. Points are matched using
173 a RANSAC-based algorithm. Our RANSAC-based method is based on match-
174 ing randomly selected points on the object trajectories of synchronized thermal
175 and visible videos, and finding the best matching points. The affine transforma-
176 tion matrix H is estimated using the normalized Direct Linear Transform (DLT)
177 method [21] to find the least squares solution.

178 A pair of trajectories is composed of a trajectory from the thermal video and
179 another from the visible video. For example, at frame t , if there are three trajec-
180 tories for thermal video (T_{left}^1 , T_{left}^2 and T_{left}^3) and if there are two trajectories for
181 visible video (T_{right}^1 and T_{right}^2), then we have six pairs of trajectories that are used
182 as the data pool for the RANSAC algorithm. We used the top-most point position
183 of the human silhouette during tracking to construct a trajectory, since it is less
184 sensitive to shadows on the floor that are falsely detected as part of the human
185 silhouette. Fig. 4 shows matching trajectory points of a pair of trajectories.

186 Since the videos are synchronized, a pair of corresponding trajectory points in
187 a trajectory pair is a pair of points with the same time stamp. Matching a possible
188 pair of points with the same time stamp, instead of all the points, reduces the
189 combinatorial complexity of the matching problem considerably.

190 Our RANSAC algorithm is a non deterministic iterative algorithm that esti-
191 mates the transformation matrix based on the matching of object trajectory points

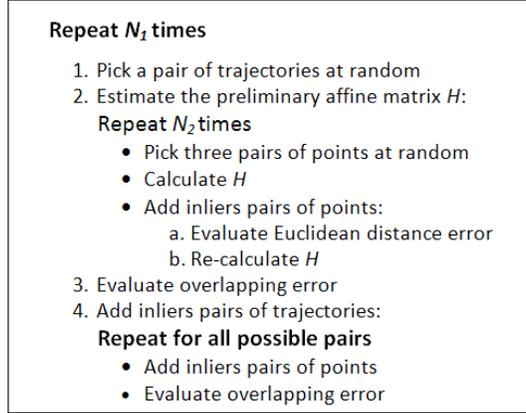


Figure 3: RANSAC-based algorithm for trajectory point matching

192 from a pair of thermal and visible videos. Fig. 3 shows the steps of our object tra-
 193 jectory point matching. It is composed of two RANSAC loops, one for the pairs
 194 of trajectories with N_1 iterations, and one for the pairs of points in a selected pair
 195 of trajectories with N_2 iterations. The number of iterations N is computed with

$$N = \frac{\log(1-p)}{\log(1-(1-\varepsilon)^s)}, \quad (1)$$

196 where p is the confidence (in our experiments p is 0.99) and s is the minimum
 197 number of points required for the homography (e.g. $s = 3$ for affine transforma-
 198 tion). ε , the probability of outliers, is computed by

$$\varepsilon = 1 - \frac{N_p}{N_t}, \quad (2)$$

199 where N_p is the number of inlier pairs of points/trajectories and N_t is the total
 200 number of pairs of points/trajectories. In fact, the number of iterations depends
 201 on the number of inlier pairs of points/trajectories. The larger the number of inlier
 202 pairs, the less iteration is required. In our algorithm (Fig. 3), N_1 and N_2 are
 203 determined by Eq. 1 and 2.

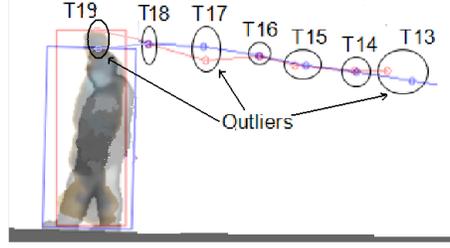


Figure 4: Matching trajectory points from thermal and visible video. T_{14} , T_{15} , T_{16} , T_{18} , and T_{19} are inliers.

204 H is calculated using three pairs of points selected at random. After that, all
 205 the points of the trajectory of the thermal video frame are transformed using the
 206 estimated H . Then, the Euclidean distance between these transformed points, and
 207 their corresponding points in the visible video are computed. Pairs of points for
 208 which the Euclidean distance is smaller than a threshold T (typically, $T = 5$ pixels)
 209 are considered as inlier pairs. The best estimation of H is that computed with the
 210 largest number of inlier pairs of points. H is re-estimated using all the inliers pairs
 211 of points. Fig. 4 illustrates the matching of selected pairs of trajectory points.

212 After the first estimation of the transformation matrix H , its quality is evalu-
 213 ated using an overlapping error function OE defined for the foreground pixels of
 214 the pairs of thermal and visible video frames.

$$OE = 1 - \frac{N_{c \cap t}}{N_{c \cup t}}, \quad (3)$$

215 where $N_{c \cap t}$ is the number of overlapping foreground color and thermal image
 216 pixels, and $N_{c \cup t}$ is the number of foreground pixels from the union of the color and
 217 thermal images. Evaluating the overlapping error allows our method to perform,
 218 even when there are few trajectories in the scene.

219 For each possible pair of trajectories, the thermal image trajectory points are

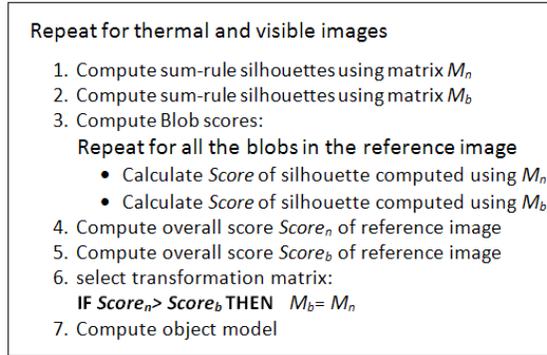


Figure 5: Our sensor fusion algorithm

220 transformed into visible image coordinates, and then the inlier pairs of points
 221 are selected using Eq. 3. Using all inlier points, the H matrix is recalculated.
 222 Then, the overlapping error is computed for the new estimated matrix H . If the
 223 overlapping error for the new estimated matrix is less than the overlapping error
 224 of the previous estimation of H , the pair of trajectories is added to the set of inlier
 225 pairs of trajectories. This procedure is continued until all the possible pairs of
 226 trajectories have been evaluated.

227 5. Thermal-visible sensor fusion

228 Thermal-visible sensor fusion combines the information of the registered color
 229 and thermal foreground images. Fig. 5 shows our sensor fusion algorithm. M_n
 230 represents the transformation matrix estimated by image registration in the current
 231 frame, and M_b represents the current best matrix. If the image registration is not
 232 performed in the current frame, computations related to M_n shown in 5 are simply
 233 skipped.

234 In this work, a silhouette is defined as a binary object region, and a sum-rule

235 silhouette is defined as a silhouette constructed using a sum of probabilities of
 236 foreground pixels in thermal and visible images. To compute a sum-rule silhou-
 237 ette, either foreground pixel coordinates of the thermal image should be trans-
 238 formed into visible image coordinates, or vice versa. Using either method, the
 239 computed sum-rule silhouette is the same. The sum-rule method was proposed by
 240 [22], and is defined as

$$(X, Y) \in S : \mathbf{IF} \ P(S | t(X, Y)) + P(S | c(X, Y)) > \alpha_{sum}, \quad (4)$$

241 where $t(X, Y)$ represents the thermal value at image coordinates (X, Y) , $c(X, Y)$
 242 represents the color value at image coordinates (X, Y) after transformation, S rep-
 243 represents the sum-rule silhouette, and α_{sum} represents a threshold. The probabilities
 244 that a pixel belongs to the foreground in each sensor are computed as

$$P(S|t(X, Y)) = 1 - e^{-\|t(X, Y) - \mu_t(X, Y)\|^2} \quad (5)$$

245 where $\mu_t(X, Y)$ is the mean background value of the coordinates (X, Y) for the
 246 thermal. $P(S|c(X, Y))$ is computed similarly for transformed visible image. The
 247 quality of a sum-rule silhouette is evaluated using a score function. A transfor-
 248 mation matrix is selected, based on the scoring results of all the silhouettes inside
 249 one image. The score function for the thermal image is defined as follows:

$$SF_t(i) = \frac{\text{sum} \left(B_{j \in \{1, \dots, n\}}^t \cap S_i^t \right)}{\text{sum} \left(B_{j \in \{1, \dots, n\}}^t \right)}, i \in \{1, \dots, m\} \quad (6)$$

250 where m is the number of computed sum-rule silhouettes inside the intersect-
 251 ing FOVs of the two cameras, S_i^t represents the i^{th} sum-rule silhouette computed
 252 in the thermal image, $SF_t(i)$ represents its score, and B_j^t are blobs in the original

253 thermal foreground image that intersect with S_i^t . Since background subtraction is
 254 not perfect, object regions might be fragmented into smaller ones in the original
 255 foreground image. So, the blobs B_j^t that intersect S_i^t should all be fragments be-
 256 longing to one object. If all blobs B_j^t are inside S_i^t , then S_i^t is perfectly aligned and
 257 its score will be 1 (the maximum value). The same applies for visible images for
 258 computation of score function in visible $SF_c(i)$. The score of matrix M_n for one
 259 image is,

$$Score_n = \left\{ \frac{\sum_{i=1}^m (SF_c(i) + SF_t(i))}{2 \times m} \right\}_{M_n} \quad (7)$$

260 where m is the number of sum-rule silhouettes, $Score_n$ is the score of matrix
 261 M_n . The $Score_b$ (the score of matrix M_b for one image) is computed similarly using
 262 matrix M_b . Finally, if the score $Score_n$ of the new estimated matrix is higher than
 263 the score $Score_b$ of the best matrix, M_n replaces M_b .

264 Blobs are also constructed. In our work, a blob is defined as all the pixels
 265 (either connected or disconnected) with their visual features that belong to one
 266 object in an image. Blobs are the input data of tracking step. The sensor fusion
 267 improves the quality of input data by computing a sum-rule silhouette that han-
 268 dles the shortcomings of the background subtraction using a single sensor, such
 269 as blob fragmentation. Furthermore, sensor fusion provides the color and ther-
 270 mal information of the blob pixels that are used as features for tracking. For blob
 271 construction, if the score of a sum-rule silhouette (Eq. 6) is maximum which is
 272 1, the sum-rule silhouette will be considered as a detected blob in the reference
 273 image. Otherwise, the original blob's fragments computed by background sub-
 274 traction that intersect with the computed sum-rule silhouette will be clustered as
 275 one blob. In this way, the fragmentation problem is solved.

276 **6. Multiple people tracking method**

277 The object model used in our tracking method is the color-thermal histogram
278 of the input blobs. This histogram has 54 bins for the HSV colors and 16 bins
279 for the thermal intensities. For tracking, any method that computes and updates
280 the trajectory of the objects frame by frame is applicable. Here, we use an online
281 Multiple Hypothesis Tracking (MHT) method, which we proposed in previous
282 work [23]. Our tracking method identifies objects at each frame and estimates
283 the best trajectories computed up to the current frame. In our previous work [23],
284 the tracking was performed only for videos captured by a single visible camera.
285 Therefore, we presented a method for handling blob fragmentation that used the
286 spatial and temporal characteristics of blobs for a few frames, in order to reattach
287 the blob fragments belonging to one object. In this work, instead of this fragmen-
288 tation handling method, we applied data fusion, which combines the information
289 from the thermal and color videos and improves the quality of the input data for
290 tracking, and, consequently, improves the tracking results considerably. Track-
291 ing is performed separately for thermal and visible videos using constructed blobs
292 with thermal-visible histogram as tracking feature.

293 Our tracking algorithm has three main steps that are described in the following
294 sections. We use two graphs for tracking: an event graph to record all blob's
295 events and store their appearance information while they are being tracked, and
296 a hypothesis graph to generate hypotheses for handling data association of split
297 objects.

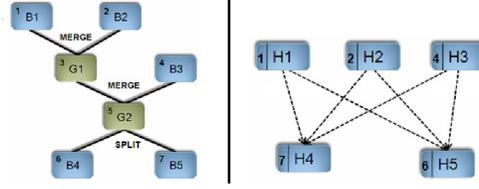


Figure 6: Event graph (left) and hypothesis graph (right). In the hypothesis graph, the number on the left of each hypothesis node corresponds to a track node in the event graph, with the corresponding number in the upper left corner.

298 6.1. Definition of event graph and hypothesis graph

299 Fig. 6 shows an event graph with its corresponding hypothesis graph. The
 300 event graph represents all blobs with their merging and splitting events during
 301 tracking. Each vertex of this graph (track node) stores a blob’s appearance, in-
 302 cluding top-most point coordinates, its adaptive thermal-color histogram, blob
 303 events such as correspondence, merging, and splitting, and the frame number of
 304 the last update in the node. Edges represent merging and splitting events among
 305 the blobs. The hypothesis graph is a directed, weighted graph. The vertices of this
 306 graph (hypothesis nodes) simply correspond to the track nodes of the event graph
 307 that belong to entering blobs (blobs that appear in the scene) and split blobs (blobs
 308 that break away from a group, or a single blob). A group blob does not have hy-
 309 pothesis nodes. This is because these nodes are used to solve the data association
 310 problem before and after object interactions. The weight of each edge $n_i n_j$ that
 311 represents a hypothesis is defined as,

$$\omega(n_i n_j) = |AH(n_i) - AH(n_j)|, \quad (8)$$

312 where $\omega(n_i n_j)$ is the Euclidean distance between two adaptive color-thermal his-
 313 tograms of the two blobs belonging to the hypothesis nodes n_i and n_j . In practice,

314 the edge information is stored in the nodes. Thus, for each hypothesis node n_i ,
 315 three sets of nodes, called S (Source), E (End), and BH (Best Hypotheses), are
 316 defined as,

$$S(n_i) = \{\forall n_j | \exists n_j n_i\}, \quad (9)$$

$$E(n_i) = \{\forall n_k | \exists n_i n_k\} \text{ and} \quad (10)$$

$$BH(n_i) = \{\forall n_j \in S(n_i) | E_1(n_j) = n_i\}. \quad (11)$$

317 The sets defined by Eq. 9 and Eq. 10 are ordered increasingly based on the
 318 weights of their common edges with n_i . In Eq. 11, BH can be empty or contain one
 319 or more elements. E_1 is the first element of E . The sets S , E , and BH are used for
 320 object labelling and for finding trajectories. It is important to note that the event
 321 graph and the hypothesis graph may be composed of more than one component
 322 (subgraph), since the connections between nodes represent the interactions that
 323 have occurred between the blobs during tracking (two blobs that do not interact
 324 are not connected).

325 6.2. Step1: matching blobs

326 In the first step of our algorithm, a distance matrix is computed to find the
 327 blobs $B_i(t-1)$ and $B_j(t)$ that possibly correspond, along with their appearance
 328 dissimilarities in two consecutive frames. The appearance dissimilarity $D_{t-1}^t(i, j)$
 329 is defined as

$$D_{t-1}^t(i, j) = \begin{cases} d(h_{B_i(t-1)}, h_{B_j(t)}) & \text{if overlapped} \\ -1 & \text{otherwise} \end{cases}, \quad (12)$$

330 where $d(h_{B_i(t-1)}, h_{B_j(t)})$ is the thermal-color histogram intersection between the
 331 i th blob in frame $t - 1$ and the j th blob in frame t if the bounding boxes of the
 332 two blobs overlap. Otherwise, these two blobs cannot match each other and their
 333 corresponding element in the matrix is -1 . This assumption is based on the fact
 334 that a blob should move on a short distance in two consecutive frames because of
 335 the frame rate of the camera. Therefore, its bounding boxes in the previous and
 336 the current frames should overlap. The size of the distance matrix is $N \times M$, where
 337 N is the number of blobs in the frame $t - 1$ and M is the number of blobs in the
 338 frame t . The thermal-color histogram intersection is defined as

$$d(h_{B_i(t-1)}, h_{B_j(t)}) = \frac{\sum_{k=1}^K \min(h_{B_i(t-1)}(k), h_{B_j(t)}(k))}{\sum_{k=1}^K h_{B_i(t-1)}(k)}, \quad (13)$$

339 where $h_{B_i(t-1)}$ and $h_{B_j(t)}$ are the thermal-color histogram of the i th blob in frame
 340 $t - 1$ and the j th blob in frame t , and K is the number of the thermal-color his-
 341 togram bins.

342 A blob in frame $t - 1$ matches a blob in frame t if the dissimilarity is not -1 .
 343 Events such as entering, leaving, merging, and splitting are detected by finding
 344 the matching blobs in two consecutive frames using the distance matrix.

345 6.3. Step 2: updating the graphs

346 The event graph and the hypothesis graph are updated based on the events
 347 detected in the matching process:

- 348 • If a blob in the current frame t is an appearing object, a track node in the
 349 event graph and a hypothesis node in the hypothesis graph are added.
- 350 • If correspondence is detected between two blobs in frames $t - 1$ and t , the
 351 track node in the event graph belonging to the object is updated by adding

352 its top-most point in the current frame t , adding the current frame number,
 353 and updating its adaptive thermal-color histogram using

$$AH_{B(t)} = \sum_{k=1}^K \alpha AH_{B(t-1)}(k) + (1 - \alpha)h_{B(t)}(k). \quad (14)$$

354 In Eq. 14, $AH_{B(t-1)}$ is the adaptive thermal-color histogram of blob B at
 355 frame $t - 1$, K is the number of thermal-color histogram bins, $h_{B(t)}$ is the
 356 thermal-color histogram of blob B at frame t , and α (varying between 0
 357 and 1) is an adaptation parameter. The adaptive thermal-color histogram is
 358 used for generating a hypothesis (likelihood between two nodes), because it
 359 gives the global thermal-color information of the blob over several frames
 360 and helps reduce the effect of dramatic changes in the thermal-color distri-
 361 bution caused by short-time variations in lighting and temperature, as well
 362 as by shadows. Updating a track node for a correspondence event is equiv-
 363 alent to a sequential data association for blobs that are not in a situation of
 364 identification uncertainty. This is based on the fact that, if two blobs, one
 365 in each of two consecutive frames are found to be similar with a mutual
 366 matching, it is very likely that they are associated with the same object.

- 367 • If some blobs in frame $t - 1$ are merged into a single blob in the current
 368 frame t , the tracking of the merging blobs is stopped and a new track node
 369 for the group blob is initiated in the event graph.
- 370 • If a blob in frame $t - 1$ has disappeared from the FOV of the camera, its
 371 track node in the event graph is deactivated.
- 372 • If splitting is detected, for each split blob a track node in the event graph

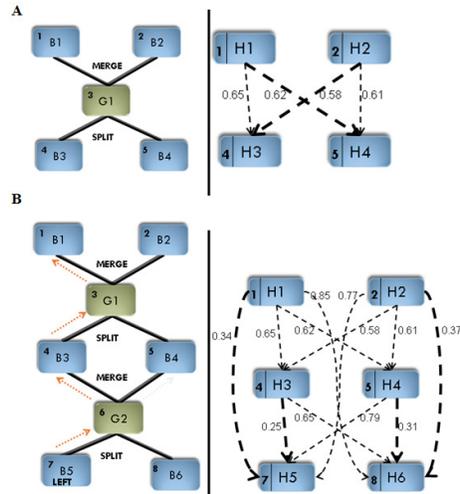


Figure 7: A) An event (left) and a hypothesis graph (right) after a merge/split. B) The same graph updated after a second merging and splitting. The number at the left of each hypothesis node corresponds to a track node in event graph with the same number in the upper left corner of the track node. The dashed arrows in the event graph show the history of one object.

373 and a hypothesis node in the hypothesis graph are added and hypotheses are
 374 generated for the newly added nodes.

375 To generate the hypotheses for split blobs, hypothesis nodes are added. Then,
 376 the S , E , and BH sets of all the nodes that are in the same subgraph as the newly
 377 added nodes are updated. Generating a hypothesis only for the nodes in the corre-
 378 sponding subgraph and not for the other nodes in the hypothesis graph is part of
 379 our strategy to reduce the number of hypotheses.

380 To perform the update, newly initiated nodes are added to the E sets of the
 381 nodes from the previous frames in the subgraph, and the previous nodes in the
 382 subgraph are added to the S sets of the newly initiated nodes. Also, the BH sets of
 383 the newly added hypothesis nodes are created according to their S sets. In other

384 words, all the nodes in the subgraph are connected, along with directed edges
 385 from the past hypothesis nodes to the new hypothesis nodes. The weight of each
 386 directed edge is the likelihood that the source node and the end node have the
 387 same appearance, and is calculated using Eq. 8.

388 If the first elements of the E sets are changed after updating (S sets and E sets
 389 are always ordered increasingly), the BH sets in the same subgraph are updated
 390 consecutively. This is based on the fact that the intersection of two BH sets for
 391 two different nodes should be empty.

392 6.4. Step 3: object labelling and trajectory computation

393 The goal of object labelling is to assign a label to each tracked blob in the
 394 current frame. For a correspondence event, the blob's label in frame t is the same
 395 as it is in frame $t - 1$. For merging, the merged blob's label in frame t is the label
 396 of all the merging blobs in frame $t - 1$. For a blob entering frame t , the label is a
 397 new one.

398 For splitting, the label of a split blob in frame t is determined by processing
 399 the hypothesis graph. To do this, we traverse the hypothesis graph in bottom-up
 400 fashion, from the current frame, starting from the split blob's hypothesis node n_i .
 401 To do this, the TN (Traversing Node) set is initialized by,

$$TN_0(n_i) = \phi, \quad (15)$$

402 and is updated by

$$TN_t(n_i) = (TN_{t-1}(n_i) \cup BH(n_{current})) - n_{next}. \quad (16)$$

403 In Eq. 16, $n_{current}$ is the current node during graph traversal (at first $n_{current}$

404 is n_i and $TN_{t-1}(n_i)$ is ϕ), $TN_t(n_i)$ is a set of possible next destination nodes in
 405 the current frame t , and n_{next} is the next node to traverse in the graph chosen with
 406 two criteria: 1) n_{next} exists in either $BH(n_{current})$ or $TN_{t-1}(n_i)$; and 2) n_{next} has
 407 the closest temporal relationship with $n_{current}$. It is important to note that, if there
 408 is more than one node in $BH(n_{current})$ or $TN_{t-1}(n_i)$ that obeys the n_{next} criteria,
 409 we traverse these nodes separately. Traversing the graph upward and updating the
 410 TN set are continued until we reach a node for which the TN set becomes empty
 411 (nowhere to go next). A split blob is given the label of the blob that we reach after
 412 traversal of the hypothesis graph. A hypothesis node belonging to a split blob that
 413 has an empty BH set before starting graph traversal is a new appearing object that
 414 is given a new label.

415 At each frame, object trajectories are computed by traversing the hypothesis
 416 graph in the same way as for labelling, to get its path into the hypothesis graph.
 417 However, in the hypothesis graph, some parts of the trajectory (when the object
 418 was tracked in a group) are missing, because group blobs have no nodes in the
 419 hypothesis graph. The missing parts of the path are recovered by completing
 420 it with the help of the event graph. Fig. 8 illustrates an example of trajectory
 421 construction for two objects that occlude each other twice.

422 7. Results and discussion

423 We have assessed the performance of our method using nine video sequences
 424 that we captured (LITIV dataset) and three video sequences of the OTCBVS
 425 dataset [11]. The LITIV dataset consists of videos of different tracking scenarios
 426 captured by a thermal and visible camera at 30 frames per second with different
 427 zoom settings and at different positions. The size of the images is 320×240 . Fig.

428 12 gives qualitative results of our unified image registration, sensor fusion, and
429 tracking. As columns (f) and (g) in the second row of Fig. 12 show, our system
430 tracks objects solely at the intersection of the FOVs of the thermal and visible
431 cameras, since sensor fusion requires the data from both sensors. In section 7.1,
432 we quantitatively assess the performance of our image registration and show that
433 our method outperforms a state-of-the-art image registration methods [3, 5]. In
434 section 7.2, we describe the quantitative results of our thermal-visible multiple
435 people tracking and show the advantage of our integrated framework which per-
436 forms multimodal tracking compared to separate tracking for thermal and visible
437 videos.

438 *7.1. Image registration evaluation*

439 We have compared our image registration method with the image registration
440 methods proposed by [3] and [5], using the same background subtraction param-
441 eters for all methods. In [3] and [5], the input data are trajectories generated
442 from separate tracking for a thermal video and a visible video without sensor fu-
443 sion. In contrast, in our method, the trajectories are generated by the tracking
444 method described in section 6 performing iteratively with our image registration
445 in a integrated framework. In [3], the registration criterion is the Euclidean point
446 error of the object trajectory points in a pair of thermal and visible videos. In
447 our proposed method and [5], foreground pixel overlapping is used as a matching
448 criterion (more details in section 4). However in [5], image registration is based
449 on a simple iterative scheme where the matrix selection is based on a simple fore-
450 ground overlapping error rather than the blob fusion score used in this work.

451 To quantitatively compare the performance of image registration methods for
452 each pair of videos, we constructed ground-truth (GT) foreground binary images

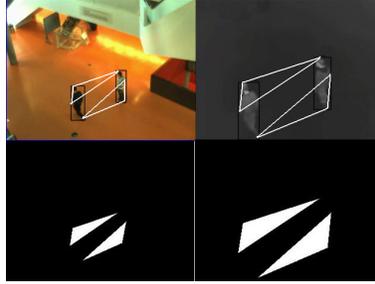


Figure 8: Top: manually selected polygons in IR and in visible images (Frame 90, Seq.1)); bottom: GT binary images

453 using a manual image registration. For the manual image registration of each pair
 454 of videos, one pair of thermal and visible video frames was manually aligned, and,
 455 based on this alignment, the affine transformation matrix was computed and used
 456 as the GT transformation matrix. Then, two GT binary foreground images are
 457 constructed by manually selecting points forming polygons on the thermal image,
 458 and by transforming the polygon's pixel coordinates of the thermal image using
 459 the GT transformation matrix to obtain a GT foreground for the visible image. Fig.
 460 8 shows the manually selected polygons and the GT thermal and visible binary
 461 foreground images. We used the GT foreground images for testing the overlapping
 462 error to ensure that the background subtraction error does not contribute to it. We
 463 used two metrics to validate our method: 1) the foreground pixel overlapping error
 464 (using an equation similar to Eq. 3) of the aligned GT foreground images using
 465 the matrices computed by our method and other two methods; and 2) the average
 466 point error, which is the average pixel coordinate error in the x and y directions of
 467 the aligned polygons' corners after transformation of the GT foreground images.

468 For foreground pixel overlapping error comparison of our method and Caspi *et*
 469 *al.* [3], we have chosen video sequence 8 of the LITIV dataset. This pair of videos



Figure 9: Top: a thermal and a visible video frames (Frame 300, Seq.8), Bottom: corresponding thermal and visible foreground images

470 is challenging because there are several long term blob fragmentations due to
 471 background subtraction misdetection and partial occlusion caused by a stationary
 472 object that is part of the background in the scene. In addition, this pair of videos
 473 is captured with a thermal and a visible camera at different zoom settings with an
 474 approximately small intersection of the FOVs, which makes image registration a
 475 challenging problem. Fig. 9 shows the blob fragmentations and the considerable
 476 object scale difference in a pair of thermal and visible image frames of video 8
 477 (frame 300).

478 Fig. 10 shows the foreground pixel overlapping error (Eq. 3) for video pair
 479 8 using our method, the method of [3], and manual image registration. Manual
 480 image registration also has a small overlapping error that is caused by rounding
 481 polygon coordinate values after transforming the points (our registration precision
 482 is in the pixel level). Around frames 350-400, due to several blob fragmentations
 483 occurring in the thermal video because of background subtraction misdetection,
 484 the overlapping error increases in the method of [3]. Also, in several frames, this
 485 method cannot estimate an acceptable transformation matrix, since the trajectories

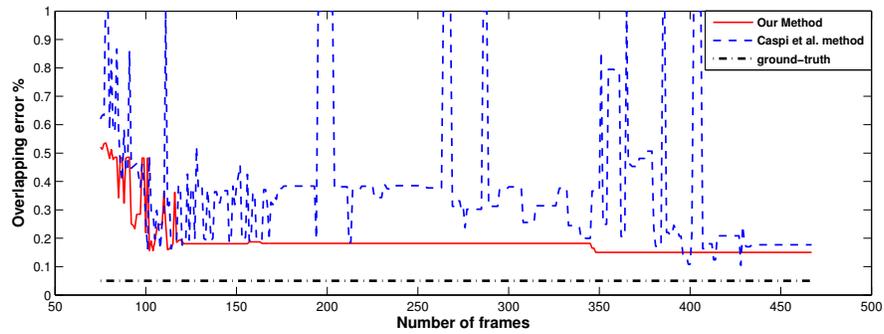


Figure 10: Overlapping error of our image registration method, of [3] image registration method, and of the manual image registration for video 8 frames 62-467.

486 in the thermal and visible videos are not similar in those frames. Therefore, the
 487 RANSAC algorithm did not succeed in estimating a transformation matrix based
 488 on matching the trajectories. In general, this plot shows: 1) our method estimates
 489 a good transformation matrix (error less than 30 percent) starting from around
 490 frames 110-120; 2) the transformation matrix estimated by our method is more
 491 stable over time compared to the method of [3], and 3) the overlapping error of
 492 our method is smaller than for the method of [3] over most video frames.

493 Our image registration, which performs iteratively with sensor fusion and
 494 tracking in a integrated system, has better image registration results than the
 495 method of [3], because: 1) the transformation matrices computed using more ac-
 496 curate trajectory points generated by tracking with sensor fusion are more precise
 497 than those computed using trajectories generated by separate tracking, because
 498 blob fragmentation is better handled; this is especially true for videos where there
 499 are several long term blob fragmentations, such as video sequence 8 (Fig. 9); 2)
 500 using the foreground pixel overlapping criterion results in good estimates of the
 501 transformation matrix, even when there is a relatively small FOV intersection; this

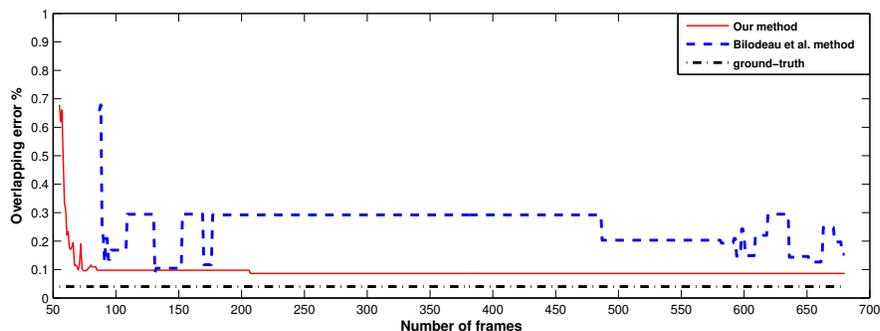


Figure 11: Overlapping error of our image registration method, of [5] image registration method, and of the manual image registration for video 1 frames 55-680.

502 makes trajectory matching a harder problem, since the trajectory patterns in the
 503 two videos are not similar, and 3) by using feedback, the matrix selection based
 504 on the fusion score (section 5) replaces the previous transformation matrix by a
 505 new one only if it has better fusion score.

506 Fig. 11 shows the foreground pixel overlapping error (Eq. 3) for video pair
 507 1 using our method, the method of [5], and manual image registration. The rea-
 508 son why we have chosen video pair 1 is because it has a larger intersection of
 509 the FOVs (more similar trajectories), which enable us to show the performance
 510 of simple matrix selection and compare it with matrix selection based on fusion
 511 score that we used in this work. Both plots in fig. 10 and 11 show the transfor-
 512 mation matrix selection in our method is more stable since there is less variation
 513 in the overlapping foreground errors compared to both state-of-the-art methods

514 [3, 5]. Fig. 11 shows that even the simple matrix selection used in [5] results in
515 more stable registration results with less foreground overlapping error variations.
516 However, because of the lack of accuracy of computed trajectories and the use of
517 more sophisticated matrix selection such as the one used in our integrated frame-
518 work, the overlapping errors vary more and even in some frames increase because
519 of erroneous matrix selection compared to the errors of our proposed method.

520 Table 1 shows the average point errors of our image registration method and
521 the [3] method for 12 video sequences. This table shows that, for video pairs
522 1, 3, 4, and 8, which are captured at considerably different zoom settings and a
523 relatively small FOV intersection (less similar trajectory patterns) in both X and
524 Y, the Euclidean distance errors of our system are less than with the [3] method.
525 This shows that our method is more robust than the [3] method in challenging
526 videos, where there are fewer similar trajectory patterns in the thermal and visible
527 videos. This is basically because of two features of our method: 1) using the
528 foreground pixel overlap criterion in the RANSAC-based algorithm; and 2) sensor
529 fusion, which handles the fragmentation and gives more similar trajectories in
530 both the thermal and visible videos. For the videos that are captured with the
531 same zoom and with about the same FOV intersection (videos 2, 5, and 7) and in
532 which there is a reasonable amount of short term blob fragmentation that does not
533 significantly change the trajectories, our method and the [3] method give similar
534 results. However, for video 6, where the FOVs of the two cameras are about the
535 same, because of long term blob fragmentation that changes the trajectory patterns
536 considerably, our method produces better results.

537 In our tests, videos from the OTCBVS dataset (videos 10, 11, and 12) are
538 considered as unregistered sequences of images. In video 11, the average point

539 errors are greater because there is only one person in this video and he is walking
540 in a straight line. Thus, all the trajectory points are collinear, and so one of the
541 assumptions required for estimating a precise affine matrix is not met.

542 7.2. Tracking evaluation

543 In this section, we quantitatively compare our tracking results using sensor fu-
544 sion with separate tracking for the visible and thermal videos, but with the same
545 data association method. In separate visible tracking, the color histogram is used
546 as the tracking feature and in separate thermal tracking, the pixel intensity his-
547 togram is used as the tracking feature. Table 2 shows the tracking results of our
548 method and separate thermal and visible video tracking.

549 False positive person identification, $+P$, mostly occurred during blob frag-
550 mentation, where a part of the human’s body is detected as a new person. This
551 can happen in the short term (1-2 frames) or the long term (several frames). As
552 shown in Table 2, our sensor fusion succeeded in reducing the $+P$ error by han-
553 dling blob fragmentation for both thermal and visible images in almost all the
554 videos. The other error is the false negative person identification, $-P$. This error
555 mostly occurs because of errors in people identification during a merge-split, or
556 partial occlusion of a person by an object in the scene, where the person is falsely
557 detected as a new object. Our system was able to reduce errors in people identifi-
558 cation during a merge-split in our tested videos. The reason is that, in our method,
559 a thermal-visible histogram is used as the tracking feature, which is more robust
560 than separate color or thermal intensity histograms.

561 In Table 2, we also quantitatively compared the trajectories generated with
562 our method and those generated by the separate video trackers using GT trajec-
563 tories generated manually. The average Euclidean distance trajectory point error,

564 AE_{ir-vi} , of our tracking method is significantly smaller than the separate visi-
565 ble/infrared trackers. This shows the effectiveness of sensor fusion for computing
566 more accurate trajectories. In fact, our video registration and tracking results show
567 that our sensor fusion plays a critical role in improving the quality of the whole
568 system.

569 **8. Conclusions**

570 In this paper, we have proposed an iterative integrated framework for thermal-
571 visible video registration, sensor fusion, and multiple people tracking method
572 with feedback designed for a pair of far-range, synchronized thermal and visi-
573 ble videos. Our video registration method is based on a RANSAC trajectory-
574 to-trajectory matching that estimates an affine transformation matrix. Our sensor
575 fusion method handles the object fragmentation caused by imperfect single sensor
576 background subtraction using the aligned thermal and visible video frame pairs.
577 Finally, our multiple people tracking methods inputs blobs constructed in sensor
578 fusion and outputs the trajectories of moving people in the scene.

579 In our result, we have shown that sensor fusion improves tracking, and ulti-
580 mately the accuracy of the object trajectories and registration. Our experiments
581 show that our method outperforms similar methods previously developed, such
582 as the [3, 5] method. Our proposed feedback scheme is flexible enough to use
583 any other tracking method that generates trajectories online, and any other sen-
584 sor fusion and object modeling that is needed for a specific video surveillance
585 application.

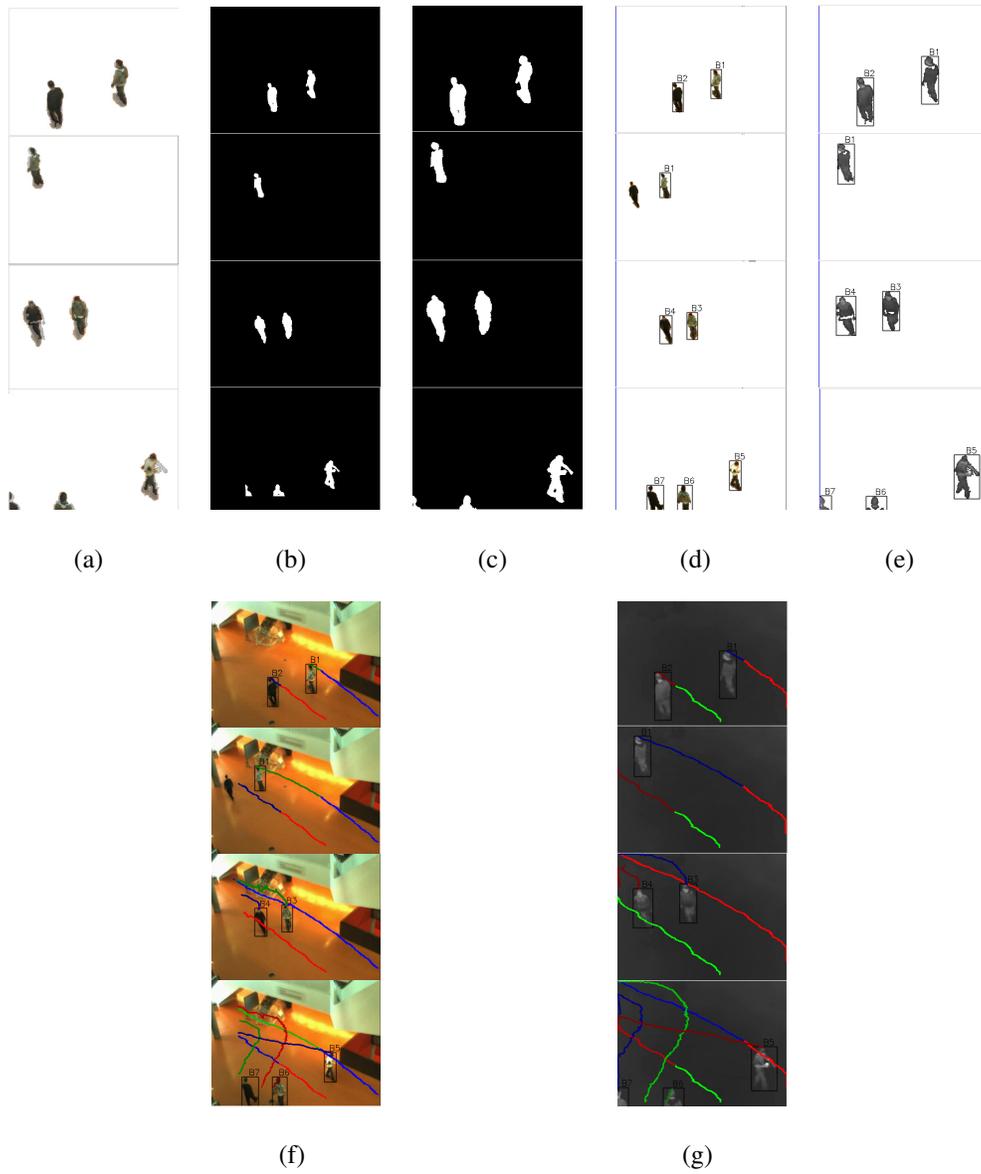


Figure 12: Our results of video 1 at frames 99, 182, 300, and 652. (a) registration of the visible on the thermal image, (b) sum-rule silhouette aligned on the visible image, (c) sum-rule silhouette aligned on the thermal image, (d) and (f) tracking result for the visible image, and (e) and (g) tracking result for the thermal image

586 **References**

- 587 [1] Z. Zhu, T. Huang, Multimodal surveillance: An introduction, in: IEEE Con-
588 ference on Computer Vision and Pattern Recognition, 2007, pp. 1–6.
- 589 [2] D. Socolinsky, Design and deployment of visible-thermal biometric surveil-
590 lance systems, in: Computer Vision and Pattern Recognition, 2007. CVPR
591 '07. IEEE Conference on, 2007, pp. 1 –2.
- 592 [3] Y. Caspi, D. Simakov, M. Irani, Feature-based sequence-to-sequence match-
593 ing, *Int. J. Comput. Vision* 68 (2006) 53–64.
- 594 [4] F. Morin, A. Torabi, G.-A. Bilodeau, Automatic registration of color and
595 infrared videos using trajectories obtained from a multiple object tracking
596 algorithm, in: Computer and Robot Vision, Canadian Conference, 2008, pp.
597 311–318.
- 598 [5] G. A. Bilodeau, A. Torabi, F. Morin, Visible and infrared image registration
599 using trajectories and composite foreground images, *Image Vision Comput.*
600 29 (2011) 41–50.
- 601 [6] A. Torabi, G. Masse, G.-A. Bilodeau, Feedback scheme for thermal-visible
602 video registration, sensor fusion, and people tracking, in: Computer Vision
603 and Pattern Recognition Workshops (CVPRW), 2010 IEEE Computer Soci-
604 ety Conference on, 2010, pp. 15 –22.
- 605 [7] C. Conaire, N. O’Connor, E. Cooke, A. Smeaton, Comparison of fusion
606 methods for thermo-visual surveillance tracking, in: 9th International Con-
607 ference on Information Fusion, 2006, pp. 1–7.

- 608 [8] F. Sadjadi, Comparative image fusion analysais, in: Proceedings of the 2005
609 IEEE Computer Society Conference on Computer Vision and Pattern Recog-
610 nition (CVPR'05) - Workshops - Volume 03, 2005, p. 8.
- 611 [9] C. O. Conaire, N. E. O'Connor, A. Smeaton, Thermo-visual feature fusion
612 for object tracking using multiple spatiogram trackers, *Mach. Vision Appl.*
613 19 (5-6) (2008) 483–494.
- 614 [10] P. Kumar, A. Mittal, P. Kumar, Addressing uncertainty in multi-modal fusion
615 for improved object detection in dynamic environment, *Information Fusion*
616 11 (4) (2010) 311 – 324.
- 617 [11] J. W. Davis, V. Sharma, Fusion-based background-subtraction using contour
618 saliency, in: *CVPR '05: IEEE Computer Society Conference on Computer*
619 *Vision and Pattern Recognition - Workshops, 2005*, pp. 11–19.
- 620 [12] J. W. Davis, V. Sharma, Background-subtraction using contour-based fusion
621 of thermal and visible imagery, *Computer Vision and Image Understanding*
622 106 (2-3) (2007) 162 – 182, special issue on *Advances in Vision Algorithms*
623 *and Systems beyond the Visible Spectrum*.
- 624 [13] A. Leykin, R. Hammoud, Robust multi-pedestrian tracking in thermal-
625 visible surveillance videos, in: *CVPRW '06: Conference on Computer Vi-*
626 *sion and Pattern Recognition Workshop, 2006*, pp. 136–144.
- 627 [14] A. Leykin, Y. Ran, Thermal-visible video fusion for moving target tracking
628 and pedestrian classification, in: *In Object Tracking and Classification in*
629 *and Beyond the Visible Spectrum Workshop at the International Conference*
630 *on Computer Vision and Pattern Recognition, 2007*, pp. 1–8.

- 631 [15] R. Hammoud, *Augmented Vision Perception in Infrared: Algorithms and*
632 *Applied Systems*, Springer Publishing Company, Incorporated, 2009.
- 633 [16] S. J. Krotosky, M. M. Trivedi, Mutual information based registration of
634 multimodal stereo videos for person tracking, *Comput. Vis. Image Underst.*
635 106 (2-3) (2007) 270–287.
- 636 [17] M. Irani, P. Anandan, Robust multi-sensor image alignment, in: *ICCV*
637 *'98: Proceedings of the Sixth International Conference on Computer Vision*,
638 1998, pp. 959–966.
- 639 [18] E. Coiras, J. Santamaria, C. Miravet, Segment-based registration technique
640 for visual-infrared images, *Optical Engineering* 39 (2000) 282–289.
- 641 [19] J. Han, B. Bhanu, Detecting moving humans using color and infrared video,
642 in: *International Conference on Multisensor Fusion*, 2003, pp. 228–233.
- 643 [20] B. Shoushtarian, H. E. Bez, A practical adaptive approach for dynamic back-
644 ground subtraction using an invariant colour model and object tracking, *Pat-*
645 *tern Recogn. Lett.* 26 (1) (2005) 5–26.
- 646 [21] R. Hartley, A. Zisserman, *Multiple view geometry in computer vision*, 2nd
647 Edition, Cambridge University Press, Cambridge, UK, 2003.
- 648 [22] J. Han, B. Bhanu, Fusion of color and infrared video for moving human
649 detection, *Pattern Recogn.* 40 (2007) 1771–1784.
- 650 [23] A. Torabi, G.-A. Bilodeau, A multiple hypothesis tracking method with frag-
651 mentation handling, in: *Computer and Robot Vision*, 2009. *CRV '09*, 2009,
652 pp. 8–15.

<i>Seq.</i>	<i>Method</i>	<i>NF</i>	<i>SF</i>	<i>NP</i>	AE_X	AE_Y
1	our method	680	54	7	0.68	2.17
	Caspi <i>et al.</i>				4.75	14.79
2	our method	698	143	3	4.14	3.37
	Caspi <i>et al.</i>				6.30	3.96
3	our method	1238	200	5	2.84	2.74
	Caspi <i>et al.</i>				5.63	4.87
4	our method	329	60	2	3.89	2.84
	Caspi <i>et al.</i>				9.85	11.97
5	our method	563	100	3	2.85	3.08
	Caspi <i>et al.</i>				4.71	16.12
6	our method	1055	100	4	4.18	5.22
	Caspi <i>et al.</i>				9.86	14.07
7	our method	895	107	4	4.38	3.61
	Caspi <i>et al.</i>				4.34	2.67
8	our method	467	100	5	3.05	2.22
	Caspi <i>et al.</i>				8.89	11.21
9	our method	400	50	3	5.61	4.89
	Caspi <i>et al.</i>				7.29	7.79
10	our method	2031	180	2	1.29	1.57
	Caspi <i>et al.</i>				1.05	2.87
11	our method	650	123	1	5.92	9.03
	Caspi <i>et al.</i>				9.36	8.33
12	our method	1302	100	3	0.83	0.37
	Caspi <i>et al.</i>				6.93	2.83

Table 1: Seqs. 1-9, videos from the LITIV dataset, and Seqs. 10-12, videos from the OTCBVS dataset [11]. Our image registration results and Caspi *et al.* [3] registration results. *NF*: number of video frames, *SF*: starting frame, which is the first frame after initialization in our method (section 4), AE_X : Average Euclidean error in X of the polygons’ corners for frames after initialization, AE_Y : Average Euclidean error in Y of the polygons’ corners for frames after initialization.

<i>Seq.</i>	<i>Method</i>	<i>NF</i>	<i>NP</i>	$-P_{ir-vi}$	$+P_{ir-vi}$	AE_{ir-vi}
1	Our method	680	7	0-0	0-0	3.57-2.12
	Separate			0-2	1-3	3.98-2.42
2	Our method	698	3	0-0	0-1	2.32-3.57
	Separate			4-4	2-1	2.74-2.47
3	Our method	1238	5	0-0	0-0	2.72-2.83
	Separate			0-4	5-0	3.27-2.74
4	Our method	329	2	0-0	0-0	5.02-3.12
	Separate			2-2	1-3	19.22-15.71
5	Our method	563	3	0-0	2-3	2.86-2.22
	Separate			2-2	3-3	2.83-3.17
6	Our method	1055	4	0-0	2-4	3.60-2.18
	Separate			0-0	4-6	10.48-7.54
7	Our method	895	4	2-2	0-3	2.27-2.46
	Separate			4-4	3-4	2.35-2.43
8	Our method	467	5	0-1	3-3	7.93-5.31
	Separate			2-1	11-8	14.56-5.26
9	Our method	400	3	0-0	2-2	3.06-4.70
	Separate			2-2	2-4	3.27-4.85
10	Our method	2031	2	0-0	1-0	2.51-1.38
	Separate			0-0	6-3	4.87-2.60
11	Our method	650	1	0-0	0-0	1.67-3.03
	Separate			0-0	4-0	1.22-1.92
12	Our method	1302	3	0-0	0-0	1.73-1.77
	Separate			0-0	3-0	0.81-0.75

Table 2: Seq.1-9, videos from the LITIV dataset and Seq. 10-12 videos from the OTCBVS dataset [11]. Our thermal-visible tracking results and separate thermal-visible tracking results without sensor fusion. *NF*: number of frames, *NP*: number of tracked people, $+P_{ir-vi}$: false positive identified number of people in thermal and visible, $-P_{ir-vi}$: false negative identified number of people in thermal and visible, and AE_{ir-vi} : Average Euclidean distance trajectory point error compared with manually generated GT trajectories.